

# Substrate Integrated Waveguide Filters Based on Dual-Mode Air-Filled Resonant Cavities

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**Abstract**—This paper presents the design and implementation of a novel class of substrate integrated waveguide (SIW) filters, based on partially air-filled cavity resonators. Removing the dielectric in a portion of the SIW cavity allows obtaining dual-mode cavities: such cavities represent a doublet, used as the building blocks in the design of filters. A thorough modal analysis of the air-filled resonant cavity based on transmission lines representation and a detailed study of the doublet permit to demonstrate a full control of the operation frequency, pass bandwidth, spurious-free region, and position of the transmission zeros of the filter. The paper presents the design, fabrication and measurement of several two-pole filters based on this concept, with the aim to show the capabilities of the proposed structure and of the design technique. A five-pole filter is also presented, to describe the extension of the proposed approach to higher order filters.

**Index Terms**— Filters, Modal analysis, Resonator filters, Substrate integrated waveguide.

## I. INTRODUCTION

THE EVOLUTION OF THE WIRELESS MARKET with the advent of the Internet of Things (IoT) and the fifth generation mobile networks (5G) is driving the microwave community towards the investigation of novel technologies, able to support the needs of the emerging applications. In particular, the requirements of the next generation of wireless systems are low cost, simple design and easy fabrication, low loss and complete integration of entire wireless systems.

These emerging applications are stimulating the research in the field of the substrate integrated waveguide (SIW) technology [1]. Based on a dielectric substrate with top and bottom metal layers and two lateral rows of conductive vias, the SIW implements the classical rectangular waveguide in planar form. Due to its nature of planar structure, the SIW can be fabricated by using the same techniques of the microstrip

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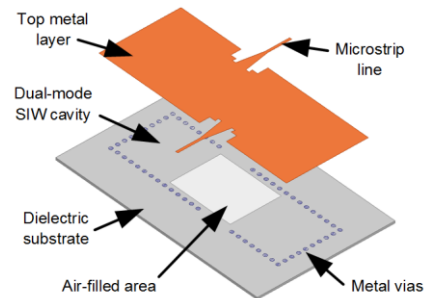


Fig. 1. Geometry of the two-pole band-pass filter (doublet) in air-filled SIW technology (from [19]).

line and coplanar waveguide circuits. On the other hand, due to its nature of rectangular waveguide, the SIW is shielded, thus preventing undesired radiation and spurious coupling, and presents lower losses than the microstrip line, due to the different electromagnetic field distribution.

SIW structures have been adopted for the design of a variety of microwave filters at different frequencies [2]-[7]. Size reduction and loss minimization are key points in the current research on SIW filters. Several alternative topologies have been proposed to reduce the footprint of SIW filters, including folded [8], half-mode [9], quarter-mode [10] and eighth-mode [6] SIW cavities. These solutions allow reducing the filter size by a factor ranging from two to eight. The price to pay is either a more complex fabrication based on a dual layer technology (in the case of the folded SIW), or higher radiation losses due to the partially open structure (in the case of half-mode and quarter-mode cavities). In the case of filters, the size reduction can also be achieved by using dual-mode resonators, which can also introduce transmission zeros by using the fundamental mode as a non-resonating mode [11]-[15]. When the main problem is the loss minimization, a possible solution is based on the air-filled SIW structure [16], [17]. In the air-filled SIW, the dielectric loss is reduced by removing part of the dielectric material inside the SIW, at the cost of a slightly larger size.

In this paper, a novel class of SIW filters is proposed, which combines the best features of dual-mode cavities and air-filled SIW (Fig. 1). By partially removing the dielectric material inside the SIW cavity, the resonance frequency of the first cavity modes can be controlled. This allows to achieve the desired frequency separation between the first and second

modes (used to define the pass band of the filter), as well as to maximize the resonance frequency of the higher modes (thus achieving maximum spurious-free bandwidth). The basic idea of this filter geometry was proposed in [18], where the air-filled SIW cavity is fed by an SIW line, and in [19], where the cavity is fed by a microstrip line. The basic concepts presented in the conference papers are widely extended here, with a thorough modal analysis of the air-filled cavity resonator allowing for the evaluation of resonant frequencies. Moreover, a detailed study of the dual-mode air-filled SIW cavity permits to demonstrate the full control of the operation frequency, pass bandwidth, spurious-free region, and position of the transmission zeros of the filter. Several prototypes of doublets are reported, to experimentally verify the proposed design strategy. Finally, the extension to higher order filters is shown by the design and experimental verification of a five-pole filter.

## II. THEORY OF DUAL-MODE AIR-FILLED CAVITY

This section presents a theoretical analysis of a dual-mode air-filled cavity. A comprehensive understanding of this building block is necessary for the design of any structure based on such elementary resonator, including filters, as demonstrated in [18]-[19] and the following sections. In [18]-[19], time-consuming eigenmode simulations were used in the design steps. Instead, in this paper, an efficient transmission line theoretical model is used to derive a characteristic equation of the air-filled cavity. The partially air-filled cavity is divided in three homogeneous portions (a central air-filled part and two external dielectric filled parts), and each portion is described as a transmission line. The equivalent waveguide approximation [1] is adopted, and therefore a solid-wall rectangular cavity is considered. Finally, a transverse resonance technique is obtained to achieve the resonance modes of the overall (piecewise homogeneous) cavity. Namely, the solution of the characteristic equation provides a relation between the  $TM_{mn0}$  mode resonant frequencies and the cavity dimensions.

Fig. 2(a) represents an air-filled cavity of overall length  $A$  and width  $B$ . The height of the cavity is small compared to  $A$  and  $B$ , as it typically happens in SIW structures. The cavity is loaded with dielectric of relative permittivity  $\epsilon_{r1}$  at its two ends, and it comprises a central air-filled region of relative permittivity  $\epsilon_{r0} = 1$  and length  $a$ . Fig. 2(b) shows the equivalent transmission line model of the cavity. The short-circuited dielectric loaded regions are represented by a homogeneous transmission line of length  $l_1 = (A-a)/2$  with  $TM_{mn0}$  mode guide impedance  $Z_{1mn0}$ , propagation constant  $\beta_{1mn0}$  and dielectric permittivity  $\epsilon_{r1} > 1$ .

The central air-filled region is modelled as two sections of length  $l_0 = a/2$  with  $TM_{mn0}$  mode guide impedance  $Z_{0mn0}$ , propagation constant  $\beta_{0mn0}$  and dielectric permittivity  $\epsilon_{r0} = 1$ . The guide impedance and propagation constant of both types of equivalent transmission lines are given by:

$$\beta_{0,1mn0} = \sqrt{(2\pi f \sqrt{\mu_0 \epsilon_0 \epsilon_{r0,1}})^2 - \left(\frac{n\pi}{B}\right)^2} \quad (1)$$

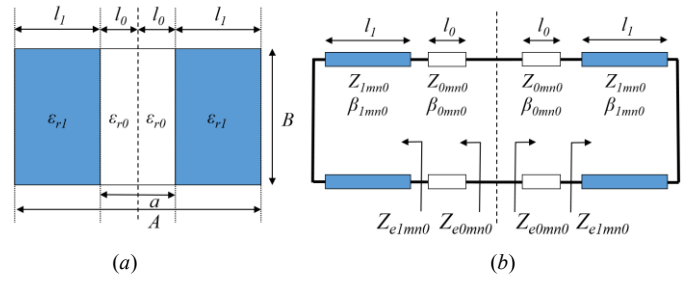


Fig. 2. (a) Top view of an air-filled cavity resonator and (b) equivalent transmission-line model.

and

$$Z_{0,1mn0} = \sqrt{\frac{\mu_0}{\epsilon_0 \epsilon_{r0,1} - \left(\frac{n}{2Bf\sqrt{\mu_0}}\right)^2}} \quad (2)$$

where  $f$  is the frequency,  $\mu_0$  is the vacuum permeability and  $\epsilon_0$  is the vacuum permittivity.

From transmission line theory, the  $Z_{e1mn0}$  equivalent impedance shown in Fig. 2(b) is determined by:

$$Z_{e1mn0} = jZ_{1mn0} \tan(\beta_{1mn0} l_1). \quad (3)$$

Then, the equivalent impedance  $Z_{e0mn0}$  at the cavity symmetry plane looking toward one side is given by:

$$Z_{e0mn0} = Z_{0mn0} \frac{Z_{e1mn0} + jZ_{0mn0} \tan(\beta_{0mn0} l_0)}{Z_{0mn0} + jZ_{e1mn0} \tan(\beta_{0mn0} l_0)}. \quad (4)$$

For odd modes (odd values of  $m$ ), at the cavity resonance  $f_{TM_{mn0}}$ , the imaginary part of (4) is:

$$\text{Im}(Z_{e0mn0}) = \infty, \quad (5)$$

whereas, for even modes (even values of  $m$ ), at the cavity resonance  $f_{TM_{mn0}}$ , the imaginary part of (4) is:

$$\text{Im}(Z_{e0mn0}) = 0. \quad (6)$$

To solve (5) and (6), the Newton-Raphson method can be used to determine the cavity resonance frequencies [20].

For illustration purposes, the following part will consider a total cavity length  $A = 50$  mm and a dielectric material of permittivity  $\epsilon_{r1} = 10.5$ . Fig. 3(a) and Fig. 3(b), reports the first four mode resonance frequencies obtained solving (5) and (6) of air-filled cavities of width  $B = 19$  mm and 22.5 mm, respectively, versus the air-filled area length  $a$ . It can be observed that the mode resonance frequencies depend on both  $a$  and  $B$  dimensions. The first two modes ( $TM_{110}$  and  $TM_{210}$ ) have very close resonant frequencies for  $a$  in the range of 10 mm to 35 mm. This is due to the fact that in the center of a dielectric-filled cavity the field of the  $TM_{110}$  mode is maximum, while that of the  $TM_{210}$  mode is null, as illustrated in Fig. 4(a). When the dielectric is removed in the central part of the cavity, this affects much more the  $TM_{110}$  mode than the  $TM_{210}$  mode, as shown in Fig. 4(b). Therefore, the resonance frequency of the  $TM_{110}$  mode increases much more than the one of the  $TM_{210}$  mode, thus decreasing the frequency separation between the two modes.

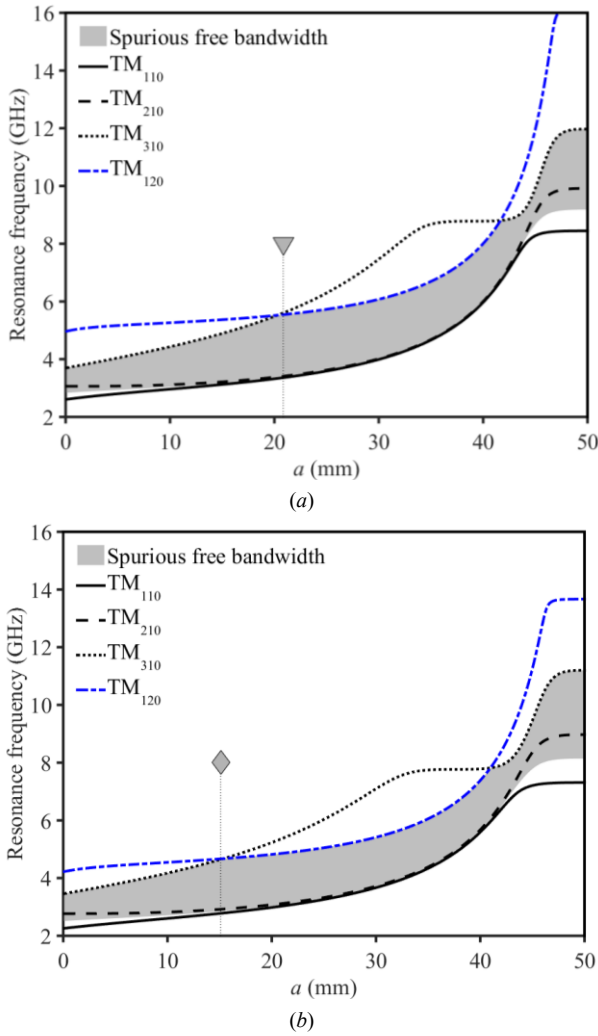


Fig. 3. Theoretical first four resonance frequencies and spurious free bandwidth versus dimension  $a$  (with  $A = 50$  mm and  $\epsilon_r = 10.5$ ): (a) For  $B = 19$  mm; (b) For  $B = 22.5$  mm.

Taking advantage of this characteristic, such air-filled cavity can be used for the design of a dual-mode cavity. By selecting the appropriate dimension  $a$  for a certain value of  $B$ , the relative frequency separation  $\Delta f$  between the  $TM_{110}$  and  $TM_{210}$  modes, given by:

$$\Delta f = \frac{2(f_{TM_{110}} f_{TM_{210}})}{f_{TM_{110}} + f_{TM_{210}}}, \quad (7)$$

and illustrated in Fig. 5, can be selected. Lower relative frequency separation can be obtained using smaller value of  $B$ . It can be seen in Fig. 5 that the percent separation decreases until the dimension of the air-filled area is about  $a = 35$  mm. Above that value, the cavity became similar to an hollow cavity, and the relative frequency separation increases significantly.

In Fig. 3, the third and fourth mode resonance frequencies are also shown. They limit the spurious-free bandwidth of the dual-mode cavity defined by the difference between the third mode resonance and the central frequency  $f_c$  of the dual-mode cavity given by:

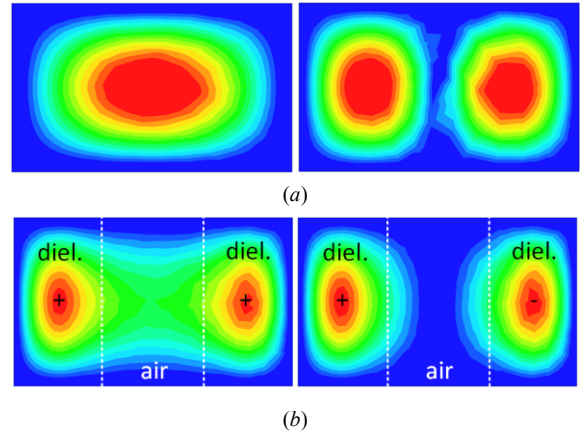


Fig. 4. Electric modal field of the first two resonant modes: (a) in dielectric-filled cavity; (b) in air-filled cavity.

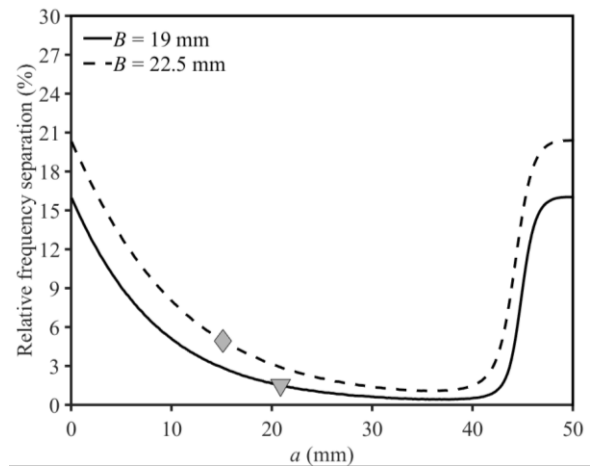


Fig. 5. Theoretical relative resonance frequency separation versus  $a$  for  $B = 19$  mm and  $22.5$  mm (with  $A = 50$  mm and  $\epsilon_r = 10.5$ ).

$$f_c = \frac{f_{TM_{110}} + f_{TM_{210}}}{2}. \quad (8)$$

It can be observed that, depending on the dimension  $a$ , the third resonance can be due to either the  $TM_{310}$  or the  $TM_{120}$  mode. The spurious-free bandwidth  $BW$ , relative to the central frequency  $f_c$  and given by:

$$BW = \frac{\min(f_{TM_{310}}, f_{TM_{120}}) - f_c}{f_c}, \quad (9)$$

is shown in Fig. 5 versus  $a$ . Optimum values are obtained for  $a = 15.1$  mm and  $B = 19$  mm ( $\blacktriangledown$  marker) and  $a = 20.85$  mm and  $B = 22.5$  mm ( $\blacklozenge$  marker), respectively. These optimum values correspond to the smallest value  $a$  in Fig. 3, at which the  $TM_{120}$  mode become the third resonating mode.

Homogeneous cavities are obtained in the particular cases of  $a = 0$  (empty cavity) and  $a = 50$  mm (dielectric filled cavity). According to Fig. 5, in homogenous cavities, the frequency separation is maximum (it is the same in case of empty and dielectric filled cavity), and it also depends on  $B$ . This suggests that the frequency separation can be controlled also in homogenous waveguide by the ratio  $A/B$ . Unfortunately, according to Fig. 3, the frequency separation

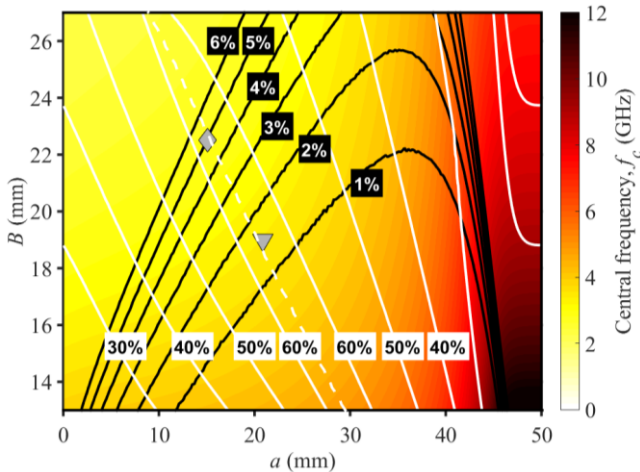


Fig. 6. Theoretical central frequency  $f_c$  with isocurves of the relative resonance frequency separation (black straight lines), relative spurious free bandwidth (white straight lines) and optimal relative spurious free bandwidth (white dotted line) versus dimensions  $a$  and  $B$  ( $A = 50$  mm,  $\epsilon_{r1} = 10.5$ ).

between third and second mode is of the same magnitude of that of second and first mode. This can be easily verified by using the formula:

$$f_{mn0} = \frac{1}{2\pi\sqrt{\mu_0\epsilon_0\epsilon_r}} \sqrt{\left(\frac{m\pi}{A}\right)^2 - \left(\frac{n\pi}{B}\right)^2} \quad (10)$$

for the evaluation of the resonance frequency of the resonant mode  $TM_{mn0}$ . This results in filters with very poor behaviour in terms of spurious free band.

Fig. 6 is a two-dimensional plot of the central frequency  $f_c$  versus dimensions  $a$  and  $B$ . It also shows isocurves of the relative resonance frequency separation (black straight lines) and relative spurious free bandwidth (white straight lines). The dimensions  $a$  and  $B$  also impact  $f_c$ . For a determined  $f_c$  and resonance frequency separation, two set of values  $a$  and  $B$  can be chosen. However, one of the two set provides a larger spurious-free bandwidth, and therefore it is more attractive for the design of a dual-mode cavity.

It can be observed in Fig. 6 that optimal relative spurious-free bandwidth (white dotted line) in excess of 60% with

TABLE I  
DIMENSIONS AND THEORETICALLY OBTAINED CHARACTERISTICS OF THE SPURIOUS FREE BANDWIDTH OPTIMIZED 1.5% AND 5% RELATIVE FREQUENCY SEPARATION DUAL-MODE CAVITIES ( $\epsilon_{r1}=10.5$ )

Two-resonance cavity	▼	◆
$A$ (mm)	50	50
$B$ (mm)   $B/A$	19   0.38	22.5   0.45
$a$ (mm)   $a/A$	20.85   0.417	15.1   0.302
$TM_{110}$ resonance frequency (GHz)	3.359	2.778
$TM_{210}$ resonance frequency (GHz)	3.410	2.919
Relative frequency separation (%)	1.5	5
Central frequency, $f_c$ (GHz)	3.385	2.849
First higher order mode resonance (GHz)	5.543	4.647
Relative spurious free bandwidth (%)	63.70	63.16

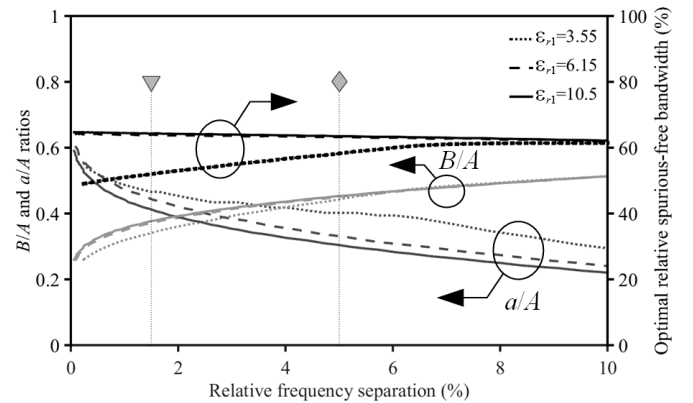


Fig. 7. Theoretical optimal spurious free bandwidth (black lines) and corresponding  $B/A$  ratio (dark gray lines) and  $a/A$  ratio (light gray lines) versus relative resonance frequency separation for  $\epsilon_{r1} = 3.55, 6.15$  and  $10.5$ .

adjustable resonance frequency separation can be obtained properly choosing the dimensions  $a$  and  $B$ .

Table I summarizes the theoretically obtained characteristics of a set of two cavities with  $\epsilon_{r1}=10.5$ , featuring 1.5% (identified in figures by a ▼ marker) and 5% (identified in figures by a ◆ marker) relative frequency separation in conjunction with the optimal relative spurious-free bandwidth.

The central frequency  $f_c$  of those optimal spurious free bandwidth dual-mode cavities can be adjusted varying the cavity overall length  $A$  while keeping constant the ratios  $B/A$  and  $a/A$ .

To achieve a desired relative resonance frequency separation, Fig. 7 provides the absolute optimal spurious-free bandwidth and corresponding ratios  $B/A$  and  $a/A$  for high, medium and low values of  $\epsilon_{r1}$  (10.5, 6.15 and 3.55, respectively). Fig. 7 represents a diagram for the design of the air-filled cavity. For this reason, on the contrary of the previous figure where a fixed value of  $A$  is used, here all considered parameters are normalized with respect to  $A$  for sake of generality. It can be observed that optimal relative resonance frequency separation values of 65% to 62% can be obtained for all three substrates. And the higher the substrate permittivity is, the higher is the optimal  $a/A$  ratio and the lower is the optimal  $B/A$  ratio.

The procedure to design an optimal spurious-free bandwidth dual-mode cavity consists in selecting in Fig. 7 the dimensional ratios for a desired relative resonance frequency separation. Then the overall cavity length  $A$  is adjusted, while keeping constant ratios to obtain the desired central frequency  $f_c$ . Further design latitude could be offered synthesizing the desired  $\epsilon_{r1}$  permittivity using either perforated substrates [21] or 3D printed materials [22].

### III. DETAILED INVESTIGATION OF THE DOUBLET

This section describes the design strategy of a doublet based on the air-filled dual-mode SIW cavity. Such doublets are capable of two poles and two transmission zeros, with the possibility to locate zero very close to the pass-band. These doublets can be used as building blocks to obtain higher-order filters with high selectivity in the upper part of the band.



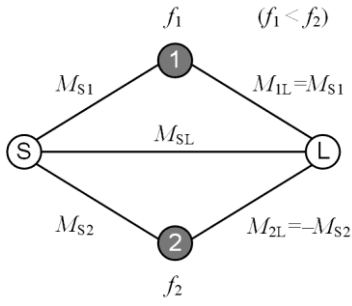


Fig. 8. Transversal topology of the doublet, implemented by using the air-filled dual-mode SIW cavity.

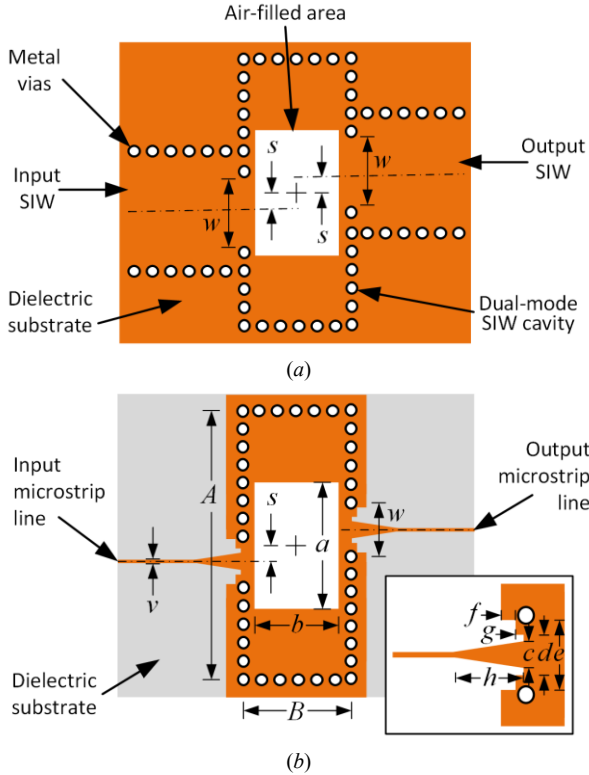


Fig. 9. Geometry of the doublet: (a) Fed by an SIW; (b) Fed by a microstrip.

### A. Implementation of the Doublet

The air-filled dual-mode SIW cavity is exploited to implement the topology shown in Fig. 8. In this topology, the filter pass band mainly depends on the resonance frequencies  $f_1$  and  $f_2$  of the first two cavity modes and, as shown in the previous section, in the air-filled SIW they are fully controllable through the dimensions of the cavity.

The external excitation of the resonator (playing the role of source S and load L in the topology of Fig. 8) can be obtained by exploiting different guiding structures. In this paper, both SIW excitation (used in [18]) and microstrip excitation (used in [19]) are discussed.

Considering the SIW feeding illustrated in Fig. 9(a), the coupling to the first two resonant modes can be controlled by the inductive iris of width  $w$ . The larger the width  $w$ , the higher the couplings values  $M_{S1}$  and  $M_{S2}$ . In case of the microstrip feeding shown in Fig. 9(b), the coupling is mainly

controlled by the microstrip taper ( $c$  and  $h$ ) and the aperture of width  $e$ .

The implementation of the topology of Fig. 8 requires three coupling values with the same sign and the fourth with an opposite sign. For this reason, in the proposed structure, the SIW and microstrip feeding lines are positioned anti-symmetrically. According to Fig. 9 and considering the symmetric distribution of the fundamental mode electric field [Fig. 4(b), left],  $M_{S1}$  and  $M_{1L}$  couplings have the identical sign. Conversely, the asymmetric distribution of the second mode electric field [Fig. 4(b), right], leads to coupling values  $M_{S2}$  and  $M_{2L}$  with opposite sign.

In the considered topology, the capability to implement and control the first transmission zero is related to the possibility of adjusting the ratio  $M_{S1}/M_{S2}$ . In both SIW and microstrip feeding lines, this ratio can be tuned by the offset  $s$  shown in Fig. 9(a) and Fig. 9(b). A second transmission zero is obtained when the direct source-to-load coupling is present. Thanks to the proximity of input and output feeding lines, this coupling is present in the proposed resonator. In fact, proximity allows some power to directly flow from input to output through higher order modes, by-passing the resonant modes. The position of this second transmission zero is not easily controlled with the proposed geometry because of the lack of degrees of freedom.

### B. Examples of Design of the Doublet

Starting from the partially air-filled dual mode cavities analyzed in Section II, some two-pole band-pass filters (doublets) have been designed, with the aim to show the full control of the relevant filter parameters.

The first doublet is based on the cavity with 1.5% relative frequency separation. The geometrical dimensions of the cavity in Table I have been used (except the transformation from effective dimensions to actual dimensions, according to the equivalent waveguide concept [1]). Only the input/output microstrip-to-SIW transitions have been optimized, in order to achieve 10 dB, 20 dB, and 30 dB pass-band input matching. The simulation results (from Ansys HFSS) are shown in Fig. 10. When the input matching is 10 dB, corresponding to a small external coupling, the position of the two poles of the frequency response, corresponding to the first two resonances of the cavity, are located at 3.355 GHz and 3.401 GHz, respectively. These values are almost coincident with the resonance frequencies of the cavity modes, reported in Table I (that are 3.359 GHz and 3.410 GHz). The resulting pass bandwidth is 1.36%. The first spurious pass band appears at 5.574 GHz, with a weak coupling of the mode supposed to resonate at 5.543 GHz in Table I. If the doublet is optimized for a better input matching, the external coupling increases, thus creating a modification of the cavity modes. Consequently, the relative frequency separation decreases, as shown in Fig. 10, and this effect needs to be accounted for in the filter design. Conversely, the spurious-free bandwidth and the position of the transmission zeros is practically unaffected by the modification of the external coupling (Fig. 10).

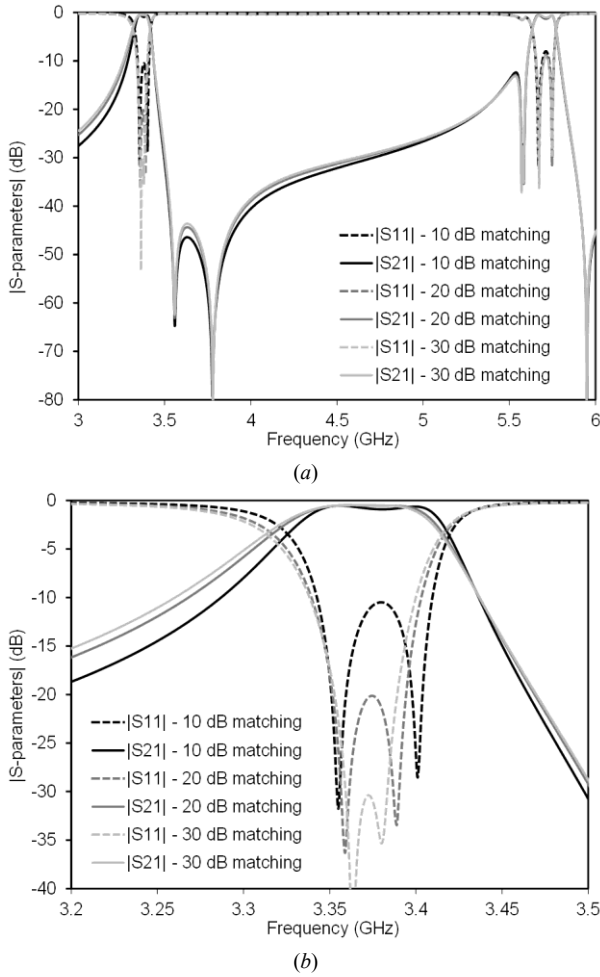
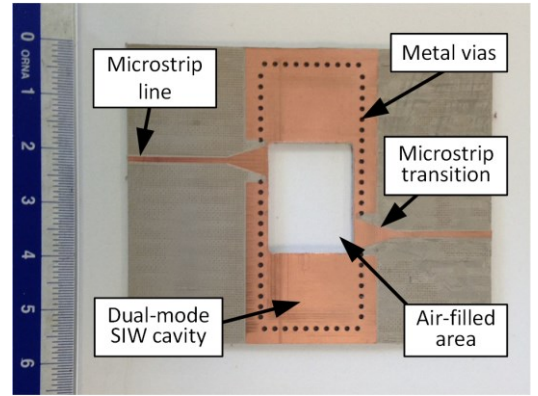


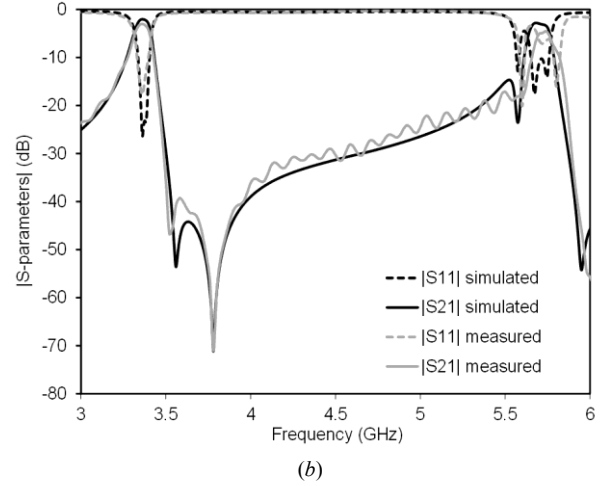
Fig. 10. Design of a two-pole filter with 1.5% relative pass bandwidth: (a) Wideband simulation of three cases, with 10 dB, 20 dB, and 30 dB input matching; (b) Detail of the pass band.

The filter with 20 dB input matching has been fabricated by milling technique on a dielectric laminate Taconic CER-10 (with relative dielectric permittivity  $\epsilon_{r1}=10.5$ , loss tangent  $\tan\delta=0.0035$ , and thickness 1.27 mm). The photograph of the prototype is shown in Fig. 11(a), before the metallization of the metal vias by using conductive paste and the closing of the top/bottom air-filled area by copper sheets. The copper sheets at the top and bottom of the air-filled area have been applied and soldered as close as possible to the perforated region. Additional details on the technology of air-filled SIW structures can be found in [16]. The filter dimensions are reported in Table II, and the width of the input/output 50- $\Omega$  microstrip line is  $v=1.27$  mm [Fig. 9(b)]. Measurements have been performed by using an Anritsu Universal Test Fixtures (UTF) 3680 and an Anritsu 37347C vector network analyzer (VNA). No de-embedding was applied to the measured results, to remove the connectors and transitions effect. The comparison between simulations and measurements is shown in Fig. 11(b). The measured insertion loss in the passband is 3.02 dB, compared to 2.04 dB in the simulation.

The same approach has been followed for the design of a second doublet, based on the cavity with 5.0% relative frequency separation, whose dimensions are shown in Table I.



(a)



(b)

Fig. 11. Validation of the design of the two-pole filter with 1.5% relative pass bandwidth and 20-dB input matching: (a) Photograph of the prototype (before vias metallization and air-filled area covering); (b) Simulation and measurement of the frequency response of the filter.

TABLE II  
DIMENSIONS OF THE FILTER WITH 1.5%  
RELATIVE FREQUENCY SEPARATION (IN MM)

$A=50.54$	$B=19.54$	$a=21.39$	$b=16.54$
$c=5.85$	$d=7.85$	$e=8$	$f=3$
$g=1$	$h=7.85$	$s=7.05$	$w=8$

Also in this case, the dimensions are not changes (with the exception of the transformation from equivalent waveguide to actual dimension). The transitions have been optimized for achieving a filtering function with 10 dB, 20 dB, and 30 dB input matching in the passband (Fig. 12). In the case of 10-dB matching (corresponding to weak external coupling), the poles of the frequency response appear at 2.664 GHz and 2.784 GHz, corresponding to a fractional bandwidth of 4.41%. If the filter is optimized to achieve a better input matching, the frequency separation decreases as in the previous example.

The filter with 20 dB input matching has been experimentally verified, by using the material, fabrication, and measurement technique previously described. The photograph of the prototype is shown in Fig. 13(a), and the filter dimensions are reported in Table III. The comparison between simulation and measurement frequency response is shown in Fig. 13(b), with an insertion loss of 1.45 dB in the measurement and of 0.88 dB in the simulation.

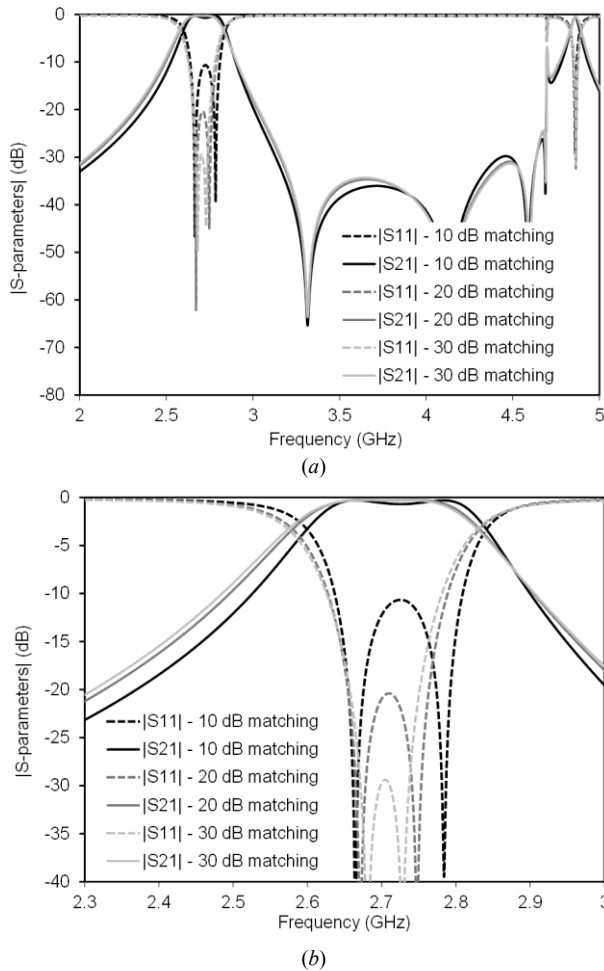


Fig. 12. Design of a two-pole filter with 5.0% relative pass bandwidth: (a) Wideband simulation of three cases, with 10 dB, 20 dB, and 30 dB input matching; (b) Detail of the pass band.

### C. Control of the Transmission Zeros

As mentioned in Section III.A, the position of the first transmission zero depends on the ratio  $M_{S1}/M_{S2}$  and it can be tuned by modifying the offset  $s$  (Fig. 9). The position of the second transmission zero depends on the direct source-to-load coupling through higher-order cavity modes, and it is also affected by the offset  $s$ . In this section, some examples are reported, to demonstrate the full control of the transmission zeros in the doublet shown in Fig. 11.

If the position of the feeding lines is centered ( $s=0$ ), only one mode of the cavity is excited by the microstrip line. As the field of the microstrip line has odd symmetry, the first cavity mode is excited and the second mode is not excited because of symmetry [Fig. 4(b)]. This results in a frequency response of the structure with one single pole [Fig. 14(a)]. The single transmission zero is due to the source-to-load coupling, which is particularly large in this case (due to proximity reasons).

Increasing the offset  $s$  of a small amount leads to the appearance of two poles (corresponding to the first two cavity modes) and two transmission zeros, one of them very close to pass band [Fig. 14(b)]. Of course, modifying the offset  $s$  allows controlling the ratio between the couplings of the

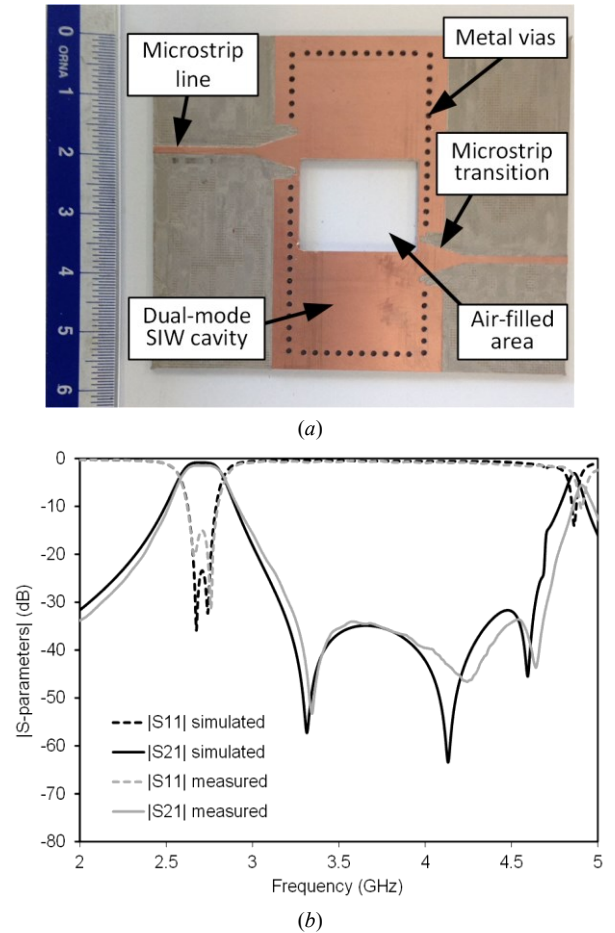


Fig. 13. Validation of the design of the two-pole filter with 5.0% relative pass bandwidth and 20-dB input matching: (a) Photograph of the prototype; (b) Simulation and measurement of the frequency response of the filter.

TABLE III  
DIMENSIONS OF THE FILTER WITH 5%  
RELATIVE FREQUENCY SEPARATION (IN MM)

$A=50.54$	$B=23.04$	$a=15.64$	$b=20.04$
$c=5.85$	$d=7.85$	$e=9$	$f=3$
$g=1$	$h=7.5$	$s=9.05$	$w=9$

two modes as well as the direct source-to-load coupling. When  $s$  increases, the ratio  $M_{S1}/M_{S2}$  decreases, due to the modal field pattern [Fig. 4(b)], and the  $M_{SL}$  coupling also decreases, due to larger separation of the input and output ports. For this reason, the position of both transmission zeros are shifted in the same direction. Two more examples are shown in Fig. 14(c) and Fig. 14(d), where the value of  $s$  is larger and the transmission zeros are shifted far from the pass band.

In all these examples, the geometrical dimensions reported in Table II have been used, with the exception of the optimization of the microstrip transition (and, of course, the offset  $s$ ).

The filter shown in Fig. 14(d) has been experimentally verified, with the fabrication and measurement described above. The photograph of the prototype is shown in Fig. 15(a), and the filter dimensions are reported in Table IV. The comparison between simulation and measurement frequency

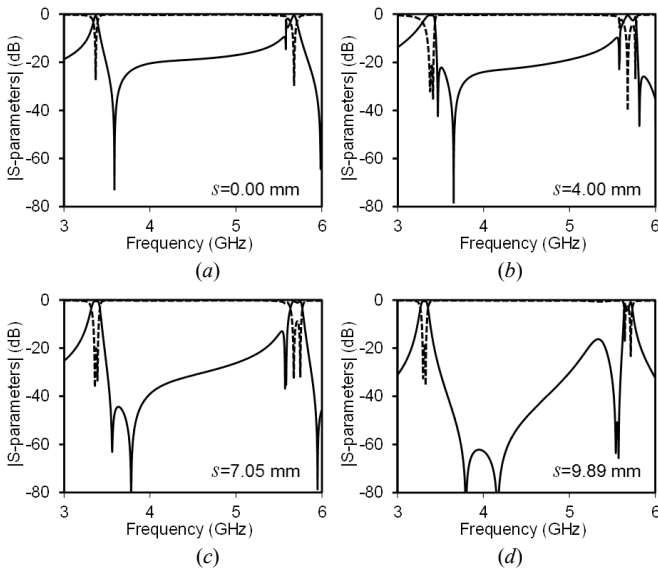


Fig. 14. Investigation of the control of the first transmission zero in the two-pole filter with 1.5% relative pass bandwidth and 20-dB input matching: (a) Symmetric structure; (b) Very close transmission zero; (c) Relatively close transmission zero; (d) Far transmission zero.

response is shown in Fig. 15(b), with an insertion loss of 2.91 dB in the measurement and of 2.21 dB in the simulation.

#### IV. DESIGN OF A HIGHER ORDER FILTER

Higher order filters can be obtained simply by cascading doublets through non-resonating nodes. This procedure allows for a modular design, where all cascaded doublets are first designed separately and then cascaded. Another advantage of this procedure is that the transmission zeros of each doublet are still present in the cascaded structure, and their position is preserved.

A simple way to implement non-resonating nodes is to use quarter-wave transmission line sections. The theory for the design of such filters has been presented in [13] and [15]. After the design, if necessary, it is possible to reduce the quarter-wave section by re-optimizing the whole filter to obtain a more compact structure.

Another possibility to cascade doublets consists in the use of half-wave sections [13]. The procedure is similar to the one based on quarter-wave sections. Modular design is still possible and position and number of doublet transmission zeros are still preserved after the cascade. The structure is larger than the one based on quarter-wave sections, but there is the advantage of obtaining an additional filter pole, being the half-wave section a resonator itself.

In order to demonstrate the feasibility of the proposed approach, a five-pole filter consisting of two doublets cascaded through a half-wave transmission line section has been designed and manufactured. The filter is centered at 2.875 GHz and its fractional bandwidth is 7.5%. The coupling matrix is provided in Fig. 16, whereas the relevant topology is shown in Fig. 17. According to Fig. 18(a), for the implementation of this topology, doublets with microstrip

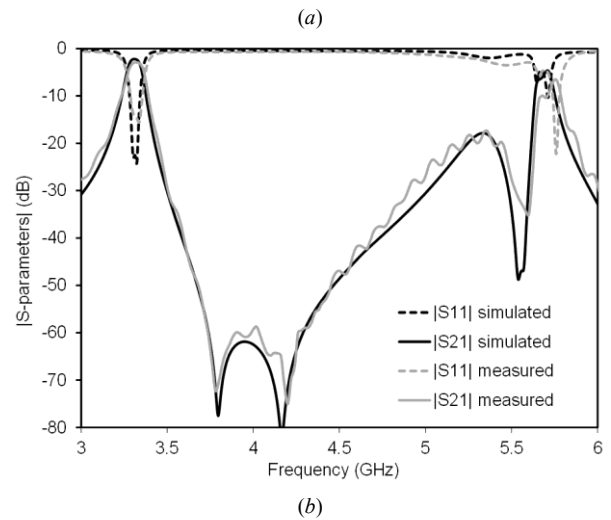
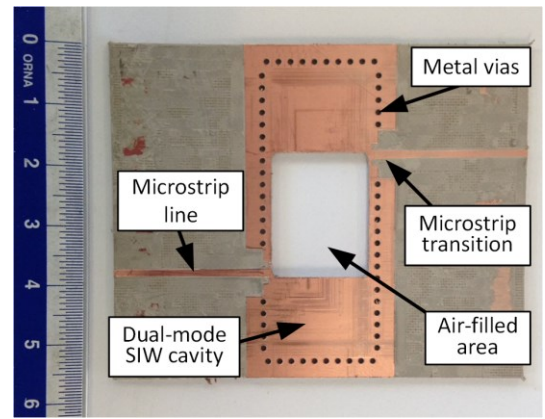


Fig. 15. Validation of the design of the two-pole filter with 1.5% relative pass bandwidth, 20-dB input matching, and far transmission zero: (a) Photograph of the prototype; (b) Simulation and measurement of the frequency response of the filter.

TABLE IV  
DIMENSIONS OF THE FILTER WITH 1.5% RELATIVE FREQUENCY SEPARATION AND SETTING OF TRANSMISSION ZEROS (IN MM)

$A=50.54$	$B=19.54$	$a=21.39$	$b=16.54$
$c=1.5$	$d=3.5$	$e=8$	$f=3$
$g=1$	$h=7.5$	$s=9.89$	$w=8$

feeding on one side and SIW feeding on the other side have been selected. This allows the five-pole filter to be fed by microstrip lines, whereas the central resonator, consisting of half-wave transmission lines, is an SIW cavity, thus obtaining better performance in terms of losses.

The manufactured prototype is shown in Fig. 18(b), while the relevant measured results are shown in Fig. 18(c), together with the full-wave simulation of the filter. Because of the symmetry of the filter, the two doublets are identical and each of them generate a transmission zero in the same position. After the cascade the position of the transmission zeros is maintained, thus resulting in a double zero in the upper stop-band. This double zero is very close to the filter band and guarantees a very high selectivity.



	S	1	2	3	4	5	L
S	0	0.949	0.509	0	0	0	0
1	0.949	0.506	0	0.799	0	0	0
2	0.509	0	-1.132	-0.056	0	0	0
3	0	0.799	-0.056	0.295	-0.056	0.799	0
4	0	0	0	-0.056	-1.132	0	0.509
5	0	0	0	0.799	0	0.506	0.949
L	0	0	0	0	0.509	0.949	0

Fig. 16. Coupling matrix of the five-pole filter, with FBW = 7.5% and central frequency at 2.875 GHz.

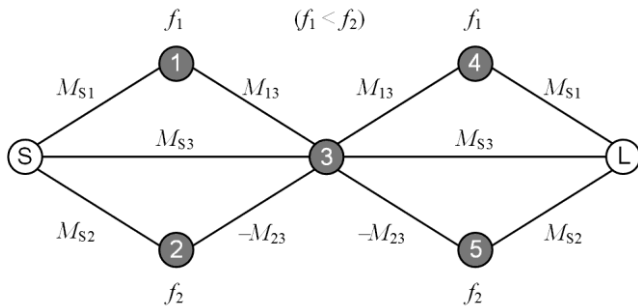


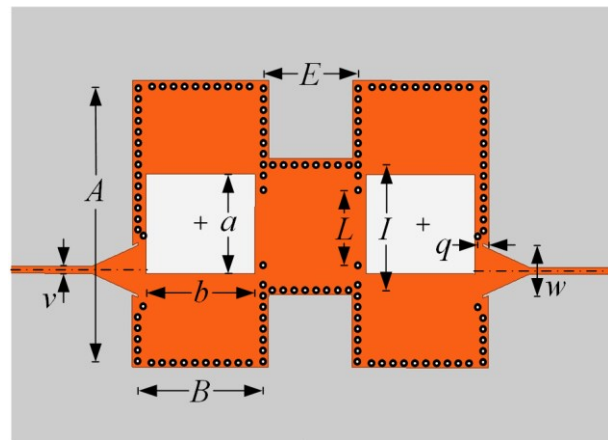
Fig. 17. Topology of the five-pole filter, based on two air-filled dual-mode SIW cavities and a standard SIW cavity.

V. CONCLUSION

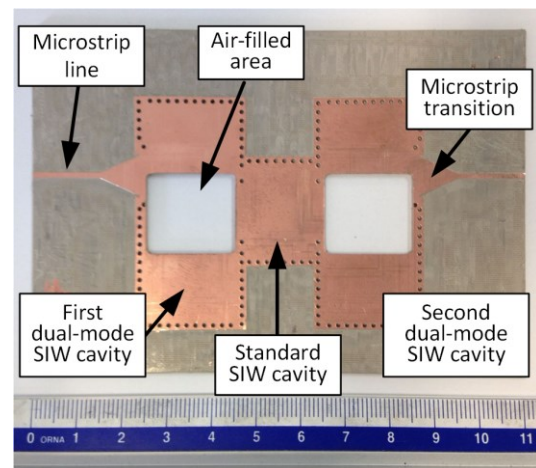
This paper presents a novel class of substrate integrated waveguide filters, which combine the advantages of the dual-mode resonant cavities with the recently proposed air-filled SIW. The basic structure proposed in this work is a doublet, able to provide two poles and two zeros in the frequency response. A detailed investigation of the doublet demonstrated how to fully control the frequency response by modifying the geometrical dimensions. In particular, the length  $A$  of the cavity allows to set the operation frequency, the size  $a$  of the air-filled region determines the pass bandwidth, the width  $B$  of the cavity controls the out-of-band, and the offset  $s$  of the input/output lines sets the position of the transmission zeros. Several prototypes have been reported to show the validity of the proposed structure, including a five-pole filter that illustrates the extension of the concept to higher-order filters.

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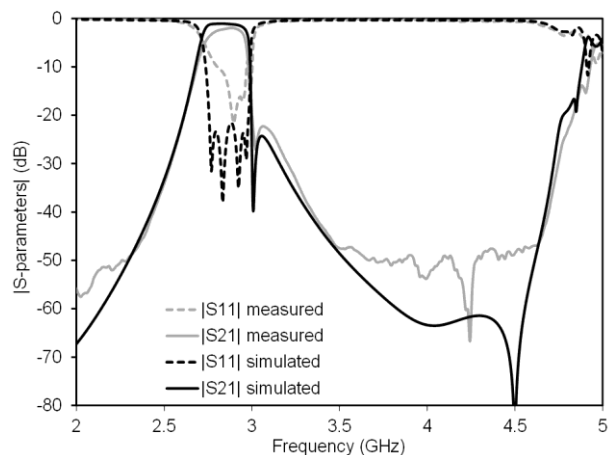
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(a)



(b)



(c)

Fig. 18. Validation of the five-pole filter: (a) Geometry of the filter; (b) Photograph of the prototype; (c) Simulation and measurement of the frequency response of the filter.

TABLE V  
DIMENSIONS OF THE FIVE-POLE FILTER (IN MM)

$A=50.54$	$B=23.04$	$a=18.2$	$b=20.04$
$c=9$	$d=10$	$e=10$	$f=1$
$g=1$	$h=8.5$	$s=8$	$w=10$
$E=17.4$	$L=13.8$	$I=22.95$	$q=2$

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