

65 Ordered Sets (SOSs) and by the work of Tankari *et al.* (2013)
 66 in the use of the rainflow counting method [13], we tailored the
 67 algorithms and match them together to find a solution to the
 68 problem of minimizing the fuel consumptions of the FOBs and
 69 optimize the BESS size, according to the operating days. No pre-
 70 vious work solved the specific problems of a FOB, except [14],
 71 which proposes the use of HOMER, but with different purposes.
 72 In this paper, a well-known mixed integer linear programming
 73 (MILP) formulation is proposed for the OEMS. Although MILP
 74 is less sophisticated than other algorithms available in the litera-
 75 ture, analysis shows that its robustness is a fundamental asset to
 76 speed up controlling strategies and obtain satisfactory results.

77 The new contribution of this paper includes the overall opti-
 78 mization procedure which uses SOSs for the semicontinu-
 79 ous function handling, and integrates economic evaluations by
 80 properly taking into account how the size of BESS affects its
 81 charge/discharge cycle; thus, the battery lifetime. Another new
 82 contribution is the hardware implementation of the optimized
 83 control system; in a laboratory prototype the OEMS coordinates
 84 the energy sources and BESS to service critical and noncritical
 85 loads using the results from the proposed optimization. It should
 86 be noted that the application of microgrid technology to FOBs is
 87 rarely found in the literature, therefore this paper is also new in
 88 the application that it presents. One important variable that must
 89 be considered in a FOB is that critical loads must be serviced
 90 at all times, even if this results in shedding of noncritical loads
 91 when a fault occurs. With the proposed algorithm, we operate
 92 to avoid the shedding. Two optimized scenarios, with and with-
 93 out a PV source, demonstrate fuel savings of $\approx 30\% - 50\%$,
 94 respectively, compared to previous work [2]. The scenarios ap-
 95 proach supports a sensitivity analysis on the amount of savings,
 96 when the PV production may fail. Experimental measurements
 97 demonstrate the OEMS functionality.

98 In Section II, the power electronics based OEMS will be
 99 illustrated. In Section III, the formulation of the optimization
 100 problem, the methodology based on SOS-constraints, and the
 101 rainflow counting method are presented to solve the minimiza-
 102 tion of the fuel consumption and for the optimal sizing of the
 103 BESS. The case study and the sizing are described and solved
 104 in Section IV, according to the operating days, conclusions are
 105 drawn in Section V.

106 II. POWER ELECTRONICS BASED EMS

107 The EMS depicted in Fig. 1 includes three inverter legs and
 108 a field programmable gate array (FPGA) based control system.
 109 Two of the legs are used for a bidirectional H-bridge converter
 110 which converts power from the dc bus to the ac loads and vice-
 111 versa. The other two legs are used for the battery pack and
 112 PV panels, respectively. Since the PV source power flows uni-
 113 directionally, only one switch and one diode of the fourth in-
 114 verter leg are used for the boost converter that conditions the
 115 PV power. The EMS includes a primary controller [15] for the
 116 power electronics and a secondary controller to manage the
 117 loads and distributed resources, including storage and PV. Solid
 118 state switches are used to connect and disconnect the two gener-
 119 ator sets (gensets) and the noncritical loads, which can be shed

120 if there is a power failure or to control peak power consumption.
 121 While Oriti *et al.* [15] focus on the EMS primary control sys-
 122 tem, this paper focuses on the secondary controller which gives
 123 the OEMS the ability to optimally manage loads and the BESS
 124 SOC.

125 III. PROBLEM FORMULATION: MILP, SOSs, AND THE 126 RAINFLOW COUNTING METHOD

127 In the following, we explain how we combine two techniques
 128 to provide an optimized secondary control law, able to answer
 129 the questions.

- 130 1) Which is the best configuration to save fuel and size bat-
 131 teries in a FOB, according to the number of operating
 132 days?
- 133 2) Which is the range of savings, if PV panels are used?
- 134 3) How can we realize it?

135 At first, we propose a formulation which improves the origi-
 136 nal setup reported in [2], second, we evolve toward a hybrid
 137 microgrid configuration, by adding the new PV plant and finally
 138 we optimize the size of the battery according to the economics
 139 and the life time of the microgrid (i.e., the operative days of
 140 the base). The results of such constrained optimization problem
 141 become instrumental for the OEMS described in the previous
 142 section. We look at a typical day, divided into j th time steps,
 143 then we base our model on two vectors of semicontinuous,
 144 nonnegative decision variables: $x_{1,j}$ and $x_{2,j}$ the average load
 145 factors of genset #1 ($P_{1r}=5$ kW, rated power) and genset #2
 146 ($P_{2r}=15$ kW), as defined in (1.5) of Table I.

147 One interesting feature in our formulation is represented by
 148 the choice to also use, as decision variable, the SOC value at the
 149 beginning of the day and impose to have the same value at the
 150 end of the day. Such choice allows us to take into account the
 151 temporal continuity, while representing a typical day. This is a
 152 neglected aspect in many papers dealing with optimization on
 153 daily profiles, although it is an important one.

154 Fig. 2 reports the linearized relationships between gensets'
 155 consumption (gal/h, 1gal = 3.79 l) and $x_{i,j}$ (and also power).
 156 Data are elaborated from an extensive research on technical
 157 datasheets from several manufacturers' websites like Caterpillar
 158 [16], Cummins [17], Kohler [18], providing gensets of suitable
 159 size for the proposed case study. Although it may seem simple
 160 to draw such relationship, a considerable effort is represented
 161 by how such data are sought and interpreted from technical
 162 datasheets.

163 We formulate an optimization problem to minimize the fuel
 164 consumption of the facility of Fig. 1, that is

$$164 \begin{aligned} f(x_{1,j}, x_{2,j}) = \\ \sum_{\substack{1 \leq i \leq 2 \\ 1 \leq j \leq J^*}} C_{i,j} = \begin{cases} m_i \cdot x_{i,j} + q_i & \text{when } x_i^m \leq x_{i,j} \leq x_i^M \\ 0 & \text{when } x_{i,j} = 0 \end{cases} \quad (1) \end{aligned}$$

165 over a J^* horizon, discretized in j time steps. m_i and q_i are
 166 the coefficients of the two linear equations in $x_{i,j}$ of the upper
 167 Fig. 2. Additional equations describing the working conditions
 168 of the diesel gensets and BESS, also with respect to photovoltaic
 169 availability, are reported in Table I with a succinct description.

TABLE I
 LIST OF VARIABLES, PARAMETERS, AND EQUATIONS DESCRIBING THE PROBLEM CONDITIONS (AT TIME j)

Variable /parameter	Description of var./param. and/or Eq.	Equations	#
$x_{1,j} - x_{2,j}$	dominion of decision variables (i.e., load factors)	$x_1^m \leq x_{1,j} \leq 1$ or $x_{1,j} = 0$	(1.2)
	no syncro condition	$x_2^m \leq x_{2,j} \leq 1$ or $x_{2,j} = 0$	(1.3)
$x_{3,j}$	battery load factor dominion	$x_{i,j} > 0 \rightarrow x_{k,j} = 0 \quad \forall k \neq i$	(1.4)
$P_{i,j}$	power from gen. and from/to BESS at time j	$-1 \leq x_{3,j} \leq 1$	(1.5)
	$(P_{1r}, P_{2r}, P_{BATmax})$	$x_{i,j} = \frac{P_{i,j}}{P_{ir}}$	(1.6)
T_{bat}, E_{bat}	time of discharge at rated P_{BATmax} and capacity of BESS	$E_{bat} = P_{BATmax} \cdot T_{bat}$	(1.7)
$L_j, P_{PV,j}$	Load and available PV power	$x_{1,j} \cdot P_{1r} + x_{2,j} \cdot P_{2r} - x_{3,j} \cdot P_{BATmax} + (P_{PV,j}) = L_j$	(1.8)
SOC_j in %	state of charge	$SOC_j = SOC_{j-1} + x_{3,j} \cdot \frac{j}{T_{bat}}$	(1.9)
	decision var.	$SOC_0 = SOC_{J^*}$	(1.10)
	dominion	$SOC^m \leq SOC_j \leq SOC^M$	(1.10)

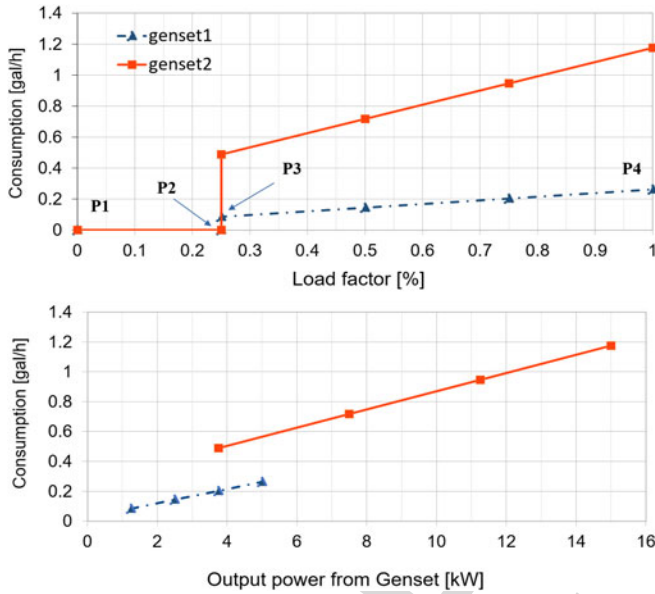


Fig. 2. Fuel consumptions (gal/h) versus load factor (%), or output power in kW for genset #1 $P_{1,r} = 5$ kW and genset #2 $P_{2,r} = 15$ kW. At the top, the coefficients of the linear equations are $m_1 = 0.2366 - q_1 = 0.0253$; $m_2 = 0.9153$. $q_2 = 0.2597$, respectively. Elaboration from [16]–[18].

170 The constraint, involving x_3 a dependant variable, means that
 171 the battery can be charged and discharged (assuming both
 172 positive and negative values), having as its hourly limit $\pm P_{BATmax}$.
 173 This condition is set to preserve its lifetime, besides charging
 174 and discharging efficiencies are set equal to 1.

175 In balancing the supply and the demand side, also the contribu-
 176 tion of the PV source ($P_{PV,j}$) can be taken into account in a
 177 deterministic way, if it exists.

178 If one of the two diesel generators can be used as a backup
 179 power to improve the reliability, no synchronization between
 180 the two gensets is required, at this stage [19].

181 Unfortunately (1) and some constraints in Table I are not
 182 straightforwardly applicable to linear programming solvers like
 183 CPLEX. The objective function (1) is a sum of the consumption

associated with the running of the two gensets

$$\begin{cases} f(x_{1,j}) = 0.2366x_{1,j} + 0.0253 \\ f(x_{2,j}) = 0.9153x_{2,j} + 0.2597 \end{cases} \quad (2)$$

185 in each time frame j th a new $x_{i,j}$ is assessed. $x_{i,j}$ can either
 186 be a value between 0.25 and 1 or be 0, so for each function
 187 $f(x_i)$, four major points can be identified by their coordinates:
 188 $P_i^1(0, 0)$, $P_i^2(0.25^-, 0)$, $P_i^3(0.25^+, m_i \cdot 0.25 + q_i)$, $P_i^4(1, m_i$
 189 $+ q_i)$ (see Fig. 2 where the points are highlighted only for genset
 190 #1). Besides, the no synchronization requirement implies that
 191 at the time j , $\forall i$

$$x_{i,j} > 0 \Leftrightarrow x_{l,j} = 0 \text{ for } l \neq i. \quad (3)$$

192 To deal with such features on decision variables, the Special
 193 Ordered Sets (SOSs), a tool in the Branch and Bound method to
 194 branch groups of variables, are introduced [20]. SOSs of type 2
 195 are functional to deal with piecewise linear continuous functions
 196 (like the objective function) and type 1 to deal with the no
 197 synchronization requirement as in [21] and [22]. The formulation
 198 of a MILP problem is thus given, from the objective function
 199 of (1) through the definition of all the conditions expressed in
 200 Table I.

A. SOSs Type 2 and Type 1 Resolution

201 $SOS2$ is an ordered set of nonnegative variables, where *no*
 202 *more than two adjacent elements can be nonzero* in a feasible
 203 solution. Consider $f(y)$, the piecewise linear function in y
 204 defined in closed intervals $[\hat{y}_k, \hat{y}_{k+1}]$, where $[\hat{y}_k, f(\hat{y}_k)]$ represent
 205 the coordinates of P_1, \dots, P_K and $k = 1, \dots, K$ (Fig. 3)

206 y in $[\hat{y}_k, \hat{y}_{k+1}]$ can be written as

$$y = \lambda_k \hat{y}_k + \lambda_{k+1} \hat{y}_{k+1} \quad (4)$$

207 where

$$\lambda_k + \lambda_{k+1} = 1 \quad \text{and} \quad \lambda_k, \lambda_{k+1} \geq 0. \quad (5)$$

208 As well, $f(y)$, linear in the interval, can be written as

$$f(y) = \lambda_k f(\hat{y}_k) + \lambda_{k+1} f(\hat{y}_{k+1}) \quad (6)$$

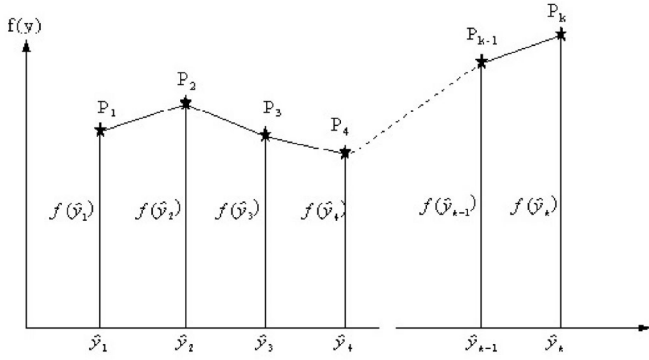


Fig. 3. Generic piecewise linear function $f(y)$ [20].

210 $f(y)$ can be represented by using a set of *weight* variables λ_k ,
 211 $k = 1, \dots, K$ as

$$f(y) = \lambda_1 f(\hat{y}_1) + \lambda_2 f(\hat{y}_2) + \dots + \lambda_K f(\hat{y}_K) \quad (7)$$

212 where

$$\hat{y}_1 \lambda_1 + \hat{y}_2 \lambda_2 + \dots + \hat{y}_K \lambda_K - y = 0 \quad y \geq 0 \quad (8)$$

$$\lambda_1 + \lambda_2 + \dots + \lambda_K = 1 \quad \lambda_k \geq 0 \quad k = 1, \dots, K. \quad (9)$$

213 Besides, we must consider the additional condition that no
 214 more than two adjacent variable can be nonzero at any time
 215 (according to [21] and [22]). These weight variables are the
 216 Special Ordered Set type 2.

217 In an electrical grid, stability is a very important issue as
 218 well as redundancy of the supply system: to provide those two
 219 requirements for a limited supply system like a FOB can be,
 220 where only a few diesel generators exist, we have been assuming
 221 that only one generator is running at a time. Taking into account
 222 such condition requires the use of SOS1. SOS1 are a set of
 223 adjacent subsequent variables where at most one element can be
 224 non zero in a feasible solution. Therefore, (9) under the condition
 225 of SOS1, that only one element can be nonzero, implies that only
 226 one element will be equal to one.

227 B. Rainflow Counting Method

228 The addition of batteries and PV sources to a traditional FOB
 229 power system leads to fuel savings and CO₂ emission reduction.
 230 As the battery size increases the fuel consumption may decrease,
 231 but the overall cost of the microgrid will go up. Therefore,
 232 battery cost and lifetime must be included in the optimization.
 233 In the economic evaluation of a given layout, the real lifetime
 234 of a battery is a sensitive parameter depending on the aging,
 235 according to the charge/discharge cycles and the DoD (Depth
 236 of Discharge). Thus, another step deals with the best sizing of
 237 the BESS, according to the typical daily working cycles. The
 238 chosen approach was an adaptation of the Miner's Rule [23],
 239 introduced by Facinelli in [24]: in brief, he observed that the
 240 higher the DoD the lower the lifetime of a battery (see Fig. 4).

241 Such rule is valid as long as the cycles do not overlap, which
 242 is typical of a simple PV+BESS configuration. When the cycles
 243 are more irregular, then the rule can not be applied as it is.
 244 For instance, this irregularity has been first found in modeling

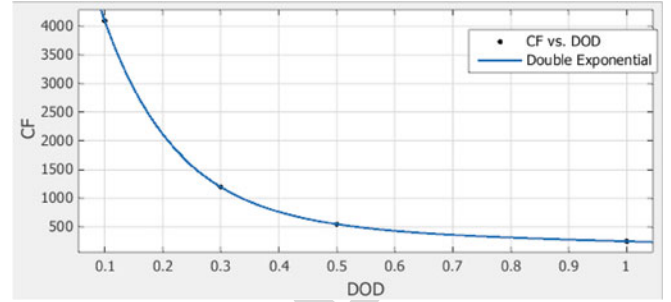


Fig. 4. Fitting curve C_F representing the cycles to failure (lifetime) of batteries versus the fractional DoD, according to data in Table II.

TABLE II
 NUMBER OF CYCLES VERSUS DoD FOR LEAD-ACID BATTERIES [29]

Depth of Discharge	# cycle (approx.)
100%	250
50%	550
30%	1200
10%	4100

Investment Costs: 1kW = 3250\$; 1.5 kW = 4125\$; 3kW = 6750\$; 5 kW=10250\$

wind/diesel kind of systems [25]. If overlapping and irregular
 245 cycles occur, the Rainflow Count, deriving from the original
 246 work of Collins [26], later resumed by [27], [28], and [13], can
 247 be used.
 248

The modeling of the wearing out of batteries due to the cycles
 249 of charge/discharge is based on considering the lifetime (cycles
 250 to failure) depending on the DoD. According to the details in
 251 Table II, the fitting curve is identified and drawn in Fig. 4.
 252

The life fraction is $1/C_F$, if after a given number of cycles
 253 the sum of the number of the cycles (N_i) multiplied by the life
 254 fraction is greater than 1, then the battery is considered being
 255 dead. In other words, the fractional damage D , defined as
 256

$$D = \sum_{i=1}^m \frac{N_i}{C_{F,i}} \quad (10)$$

is the inverse of the lifetime. The unit of measure depends on
 257 how the time horizon cycles are counted: if the DoD cycles are
 258 evaluated on a single day, then the lifetime of the battery is
 259 counted in days. The lead-acid battery characteristics of Sec-
 260 tion IV are from [29] and are reported in Table II, along with
 261 some costs, useful in the case study.
 262

The technique is based on the work of Downing *et al.* [30]
 263 and uses an algorithm created by Nielsony in MatLab code [31],
 264 where individual cycles and the range of cycles of batteries are
 265 assessed according to what is detailed in Section IV. Although
 266 the method is conceptually reasonable and it consists of the
 267 separation of cycles it must be pointed out that there is no
 268 experimental validation of it.
 269

270 IV. RESULTS FOR THE CASE STUDY OF A FOB

This section demonstrates that the optimized algorithm em-
 271 bedded in the OEMS' secondary controller reduces the overall
 272

TABLE III
RELEVANT INPUT AND OUTPUT DATA FOR BOTH THE SCENARIOS (ON A
TYPICAL DAY $J^* = 24$)

Description	Scenario n.1 (no PV)	Scenario n.2 (with PV)
$x_{1,j} - x_{2,j}$	0 or 0.25 ÷ 1 (semicont.)	0 or 0.25 ÷ 1 (semicont.)
$x_{3,j}$	-1 ÷ 1	-1 ÷ 1
$P_{1r} - P_{2r} - P_{BATmax}$ in kW	5 - 15 - 3	5 - 15 - 3
T_{bat} in h (@ $P_{BATmax} = 3kW_P$)	6	6
$SOC^m - SOC^M$ in kWh (and%)	3.6-18 (20%-100%)	3.6-18 (20%-100%)
P_{PV} peak power in kW	0	3
output		
$SOC_0 = SOC_{24}$ in %	40%	100% (see Figs. 9 and 10)
Consump. in gal/day (savings in %)	7.7 (31%)	4.65 (58%) (see Figs. 7 and 8)

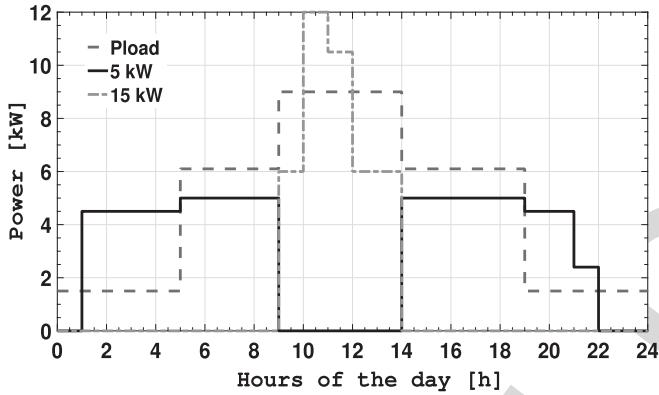


Fig. 5. Scenario n.1: Load and Power from generators (P_{BATmax} equal to 3kW, $SOC_0 = SOC_{24}$, no PV).

273 cost of the microgrid by including battery lifetime expectation
274 and a load management algorithm, more sophisticated than the
275 one presented in [2]. The experimental results are also illustrat-
276 ed.

277 A. Optimization and Cost Analysis: The Two Scenarios

278 In Table III, the most relevant input data are listed for two
279 scenarios: the first without a PV panel, to compare results with
280 the analysis in [2], the second with a 3 kW_P PV panel. At the
281 bottom of Table III, the most important outcomes from the opti-
282 mization are reported: the optimal initial SOC, the consumption
283 (gal/h), and the savings (%) against the original configuration,
284 where 11.2 gal/day (42.4 l/day) were consumed with the same set
285 of electrical loads [2]. We use two scenarios also to perform
286 a sensitivity analysis and to report a range of savings in case the
287 PV panels work or not.

288 The results of the two scenarios are reported in details from
289 Figs. 5 to 10. Figs. 5 and 6 show the power curves over a
290 24 h period for the load, for the two gensets and for the PV
291 source (only in Scenario n.2). In Scenario n.1, both gensets are
292 used but never at the same time; in Scenario n.2, the OEMS
293 chooses to use only genset #1, leaving genset #2 off. This is
294 the result of the optimization algorithm matching the loads to

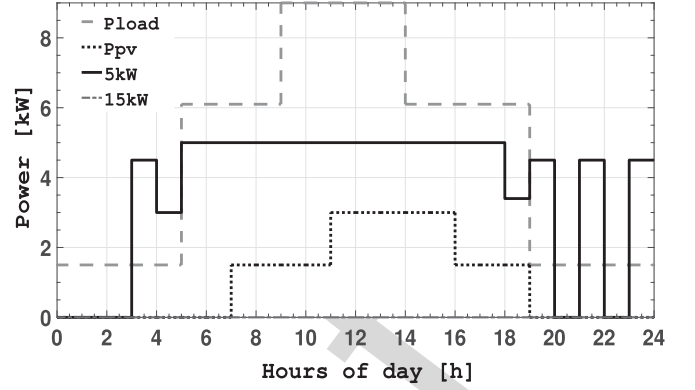


Fig. 6. Scenario n.2: Load and Power from generators (PV and P_{BATmax} both equal to 3kW, $SOC_0 = SOC_{24}$).

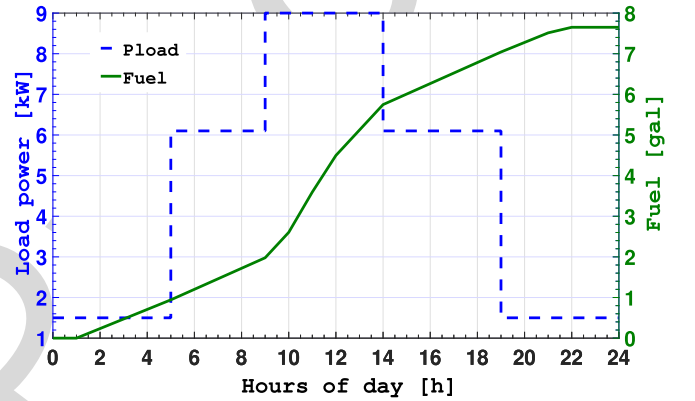


Fig. 7. Scenario n.1: Load and Consumption, power in (kW) on the primary y-axis, consumption in (gal) on the secondary y-axis (P_{BATmax} equal to 3kW, $SOC_0 = SOC_{24}$, no PV).

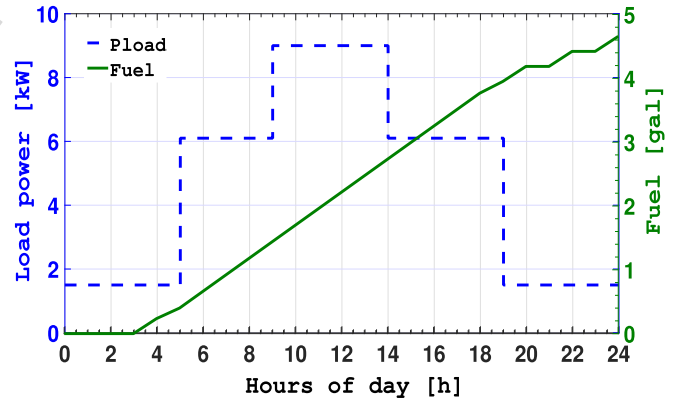


Fig. 8. Scenario n.2: Load and Consumption, power in (kW) on the primary y-axis, consumption in (gal) on the secondary y-axis (PV and P_{BATmax} both equal to 3kW, $SOC_0 = SOC_{24}$).

the sources to minimize fuel consumption, with the addition on
security of supply. The fuel consumption over the 24 h period is
plotted in Figs. 7 and 8. The total consumed fuel is 7.7 (29.15 l)
and 4.65 gallons (17.6 l), which demonstrates in both cases a
31% and 58% reduction, compared to the analysis in [2]. These
results demonstrate that the 80% derating practice, typically
used when sizing diesel generators in FOBs, is not necessary,

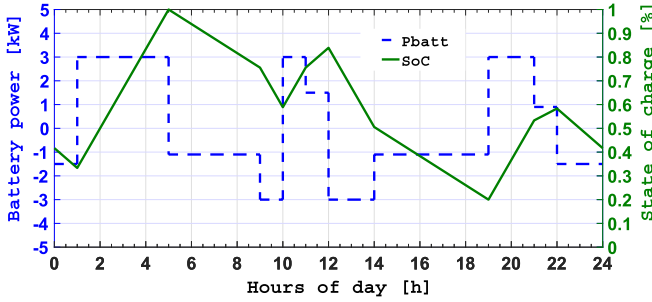


Fig. 9. Scenario n.1: Power from/to Batteries in (kW) (on primary y-axis); SOC [%] (on secondary y-axis) ($P_{BATmax} = 3kW$, $SOC_0 = SOC_{24}$, no PV). On the x-axis the hours of the typical day.

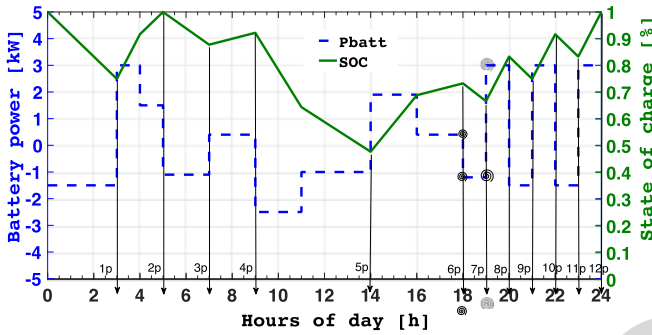


Fig. 10. Scenario n.2: Power from/to Batteries in (kW) (on primary y axis); SOC [%] (on secondary y-axis) (PV and $P_{BATmax} = 3kW$, $SOC_0 = SOC_{24} = 100\%$). On the x-axis the hours of the day and above the peaks count (from 1p to 12p). Signs at time 6 P.M.(18) and 7 P.M. (19) are recalled in Figs. 15 and 16.

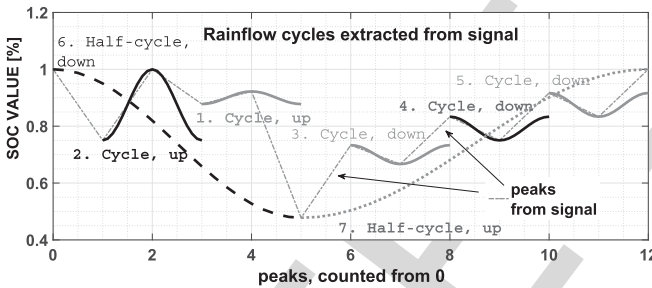


Fig. 11. Scenario n.2: identification and counting of cycles to failure. On the y-axis the SOC in % (the dotted of Fig. 10 and the superimposed peak identification and associated cycle or half-cycle) on the x-axis the peaks count.

302 because a single generator can be used at any given time, leaving
303 the second one as backup.

304 The BESS power and SOC are shown in Figs. 9 and 10, it
305 can be noted that the optimal starting SOC is different (in Sce-
306 nario n.1 is 40%, while in Scenario n.2 is 100%). The Rainflow
307 counting method is applied to the SOC of Scenario n.2 of Fig. 10
308 (on the x-axis one can read both the time of the day and the coun-
309 ting of peaks and valleys, pointed by the downward arrows) and
310 shown in Fig. 11 for the 12 major trends (up and down) deduced
311 from the scenario itself. The changes in the level of the storage
312 is resolved in individual cycles, in a given interval, and used
313 within the model of *cycles to failure* to cumulatively estimate
314 the battery wearing out. Note that the dotted line in Fig. 11
315 is the SOC curve from Fig. 10, on top of which the cycles to

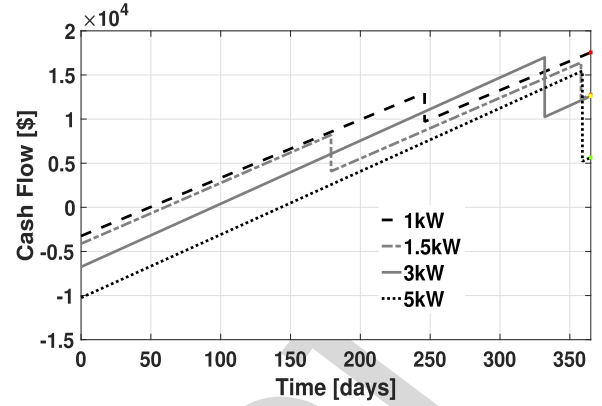


Fig. 12. Scenario n.2 (with $PV = 3kW_p$): Economic evaluation on 365 days: on the y-axis the Cash flow in [\$], on the x-axis the considered horizon [in days] for the four investigated battery sizes, investment costs from Table II and fuel cost 3.964 \$/gal.

failure for the batteries are counted. The results of the Rainflow 316
counting method are combined with the battery data in Fig. 4 to 317
create the cost analysis curves in Fig. 12, where the cash flow 318
of four different BESS sizes (1, 1.5, 3 and 5 kW) are plotted 319
versus the total number of days (the set horizon). We verified 320
and compared how the investment, which depends on the BESS 321
size, is compensated by the saving in fuel over a set horizon, 322
according to 323

$$G(\text{size, horizon}) = -\text{Inv}(\text{size}) + N_F(\text{size}) \cdot C_{\text{fuel}} \cdot \Delta\text{fuel}(\text{size, horizon}) \quad (11)$$

where G the Gain is the cash flow in \$, Inv is the investment in \$, 324
 N_F the days to failure of the batteries (depending on the number 325
and DoD of the counted cycles), C_{fuel} is the specific fuel cost 326
(\$/gal) and Δfuel is the daily difference between consumption 327
due to the traditional management of the diesel generators of [2] 328
against the optimized one (in gal/day). In this example, a 365- 329
days horizon is implemented and the 1 kW BESS is identified 330
as the most cost effective configuration because it yields the 331
greatest cash flow at the end of the year. It is worth noting that 332
if the FOB needs to be operative for less than 365 days, for 333
example, in the range between 240 and 300 days, then the 3kW 334
size BESS achieves the highest cash flow and should be used. 335

B. Experimental Set Up and Verification 336

The objective of this section is to demonstrate how the OEMS 337
hardware executes the commands sent by the optimized second- 338
ary controller presented in the previous sections. A scaled 339
laboratory prototype was built and tested that responds to the 340
four different commands. 341

- 1) While the genset is ON, switch from drawing additional 342
power from the battery bank to battery charging mode. 343
- 2) While the genset is ON, switch from battery charging mode 344
to drawing additional power from the battery bank. 345
- 3) Turnoff the genset and transition to battery-only power 346
mode. 347

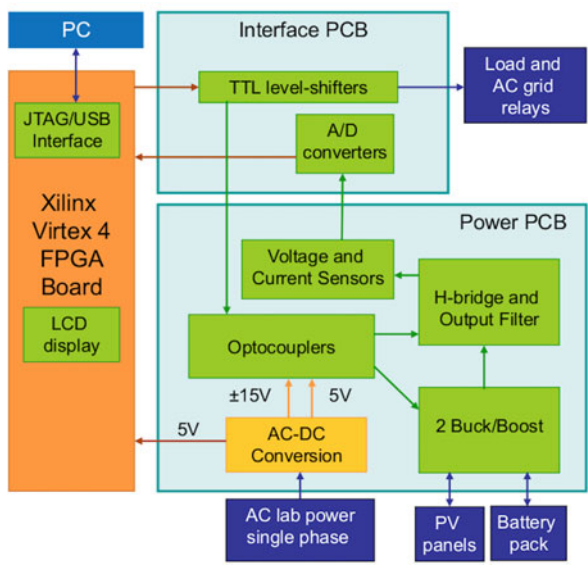


Fig. 13. OEMS hardware block diagram.

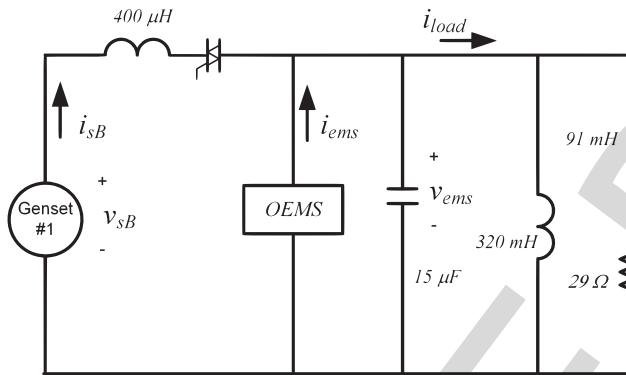


Fig. 14. Laboratory setup.

348 4) Transition from battery-only power mode to the generator
349 powering the load after the genset is turned ON.

350 The OEMS' secondary controller is responsible for such commands
351 in either of the two scenarios, with some clarifications
352 following below. The OEMS laboratory prototype includes an
353 FPGA development board, a power PCB, and an interface PCB
354 as shown in Fig. 13.

355 The OEMS power circuit is shown in Fig. 1 and further details
356 of the hardware implementation and control system can be found
357 in [15]. The circuit shown in Fig. 14 was assembled in the
358 laboratory to demonstrate how the OEMS hardware responds
359 to the secondary controller's commands. The diesel generator
360 Genset #1 was simulated by the ac grid, which provides a 120 V
361 rms voltage source, just like a diesel generator would. The power
362 level of the experiment is a few hundred watts as the main goal is
363 to demonstrate the hardware functionality, not its power rating.
364 The dc bus (shown in Fig. 1) was regulated at 200 V and lead
365 acid batteries were used for the energy storage element.

366 The voltage and current waveforms demonstrating the execution
367 of the first command of the above list are displayed in
368 Fig. 15. The load is initially powered by the generator and the
369 battery together. At $t = 0$, the OEMS reverses the power flow

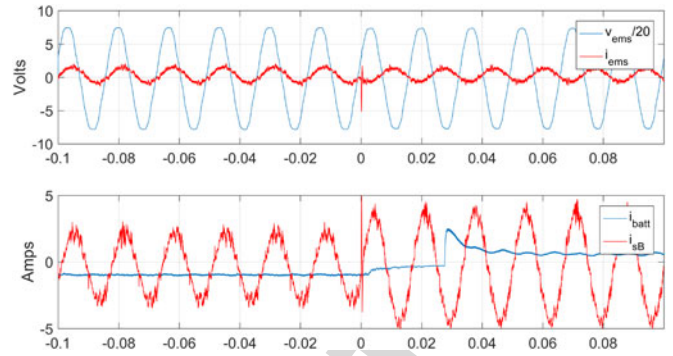


Fig. 15. Transition from drawing additional power from the battery bank to battery charging mode. The generator is kept on (see Scenario n.2 at time 7 P.M. (19:00), small spirals).

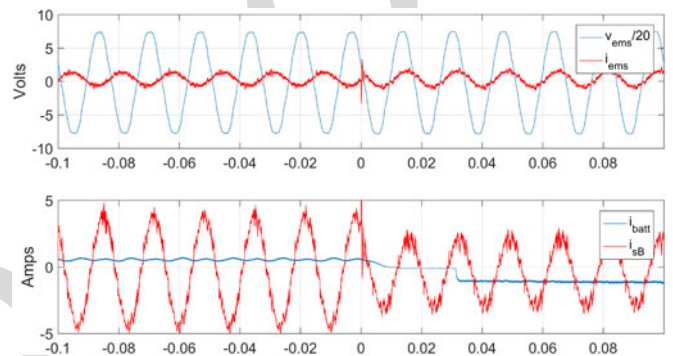


Fig. 16. Transition from battery charging mode to drawing additional power from the battery bank. The generator is kept on (see Scenario n.2 at time 6 P.M. (18:00), small spirals).

370 from/to the battery. The power flow reversal from the battery can
371 be easily identified in the top plot of Fig. 15, where the OEMS
372 current i_{ems} has a phase shift of 180° at $t = 0$ when the battery
373 quits providing power to the load and begins charging the battery.
374 The bottom plot in Fig. 15, the dc battery current goes from
375 negative (current out of the battery) to positive (current into the
376 battery) and the generator current increases to support the load
377 and the charging of the battery.

378 In Fig. 16, the voltage and current waveforms, demonstrating
379 the execution of the second command of the list, are displayed.
380 The power flow reversal is executed by the OEMS in reverse
381 order with respect to the previous experiment shown in Fig. 15.
382 Initially, the generator powers the load and charges the battery,
383 then at $t = 0$ the power flow is reversed and the battery supple-
384 ments the generator power instead of being charged.

385 The implementation of the third command of the list is dis-
386 played in Fig. 17, where the generator is turned OFF and the
387 power to the load comes only from the battery. Once again the
388 transition is transparent to the load which cannot be disrupted
389 at any time. Note that an example of this transition occurs in
390 Scenario n.1 at 9 AM where the additional turn ON of the 15 kW
391 generator does not turn ON at the same instant as the 5 kW generator
392 turns OFF, but a few seconds later.

393 In Fig. 18, the voltage and current waveforms demonstrating
394 the execution of the fourth command of the list are displayed.
395

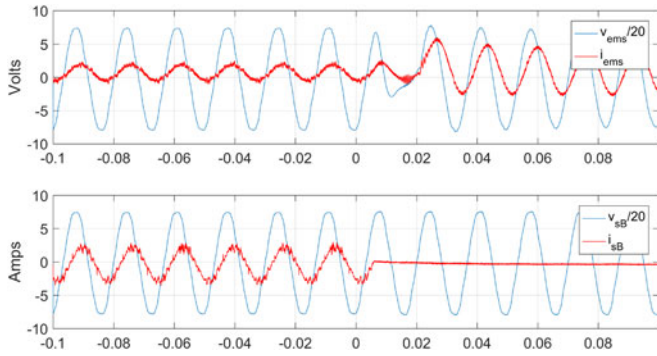


Fig. 17. Disconnect from the generator to transition into battery-only power mode.

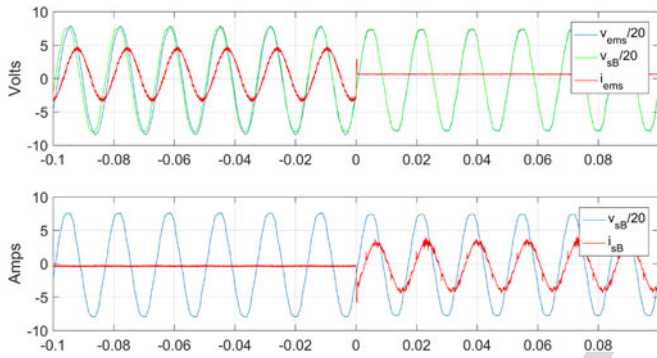


Fig. 18. Step change from battery-only power to battery and generator power after the generator is powered ON.

396 The load is initially powered only by the battery while the OEMS
 397 reduces the phase difference between the generator's voltage and
 398 its own. At $t = 0$, the OEMS latches to the generator's voltage
 399 and the load becomes powered by the generator while the OEMS
 400 current i_{ems} goes to zero. This transition is transparent to the
 401 load. Note that although there is not an example of this transition
 402 in the analyzed scenarios, this is just the first step necessary to
 403 accomplish other transitions, where the battery is subsequently
 404 charged from the generator. The complete transition does not
 405 occur instantaneously as it appears in Fig. 5 and 6, but in steps
 406 that occur within seconds or less.

407 V. CONCLUSIONS AND FUTURE WORK

408 This paper presents an OEMS which minimizes the fuel con-
 409 sumption of the diesel generators used in an FOB's micro-
 410 grid, by addressing several questions, among which the best
 411 BESS size according to the operating days of the FOB. Further-
 412 more, our formulation and solution have demonstrated that the
 413 80% derating practice, typically used when sizing diesel gener-
 414 ators in FOBs, is not necessary, because a single generator can
 415 be used at any given time, leaving the second one as backup.
 416 A MILP formulation, suitably solved by means of SOS2 and
 417 SOS1, has been successfully demonstrated. Its simplicity leads
 418 to robustness and ease of implementation. The Rainflow count-
 419 ing method was used to determine the most cost effective BESS
 420 size with a given operating time, including a 3 kW_P source.

This condition (on given operating times) thus needs to be taken
 into better account for the future operative planning of the basis.

Two 24-h scenarios were analyzed and showed fuel savings
 in the range of 30–50% with respect to a previous improved
 configuration. Such approach provides an estimate of the range
 of fuel savings, should the PV source fail. The analysis of the
 two scenarios shows that, as long as the operating days of the
 FOB are below 240 days or above 300, the best size for the
 BESS is 1 kW (6 kWh capacity), but if the operating days are
 between 240 and 300, the 3 kW battery (18 kWh capacity) is
 the best choice.

A laboratory prototype has been built to demonstrate the
 OEMS functionality. It has also been demonstrated that the
 OEMS can carry out the commands produced by the optimiza-
 tion algorithm without disturbing the bus voltage to which crit-
 ical loads are connected. Future work will analyze the impact
 of adding supercapacitors to the BESS to further increase the
 battery's lifetime and to service unexpected load transients of
 short duration.

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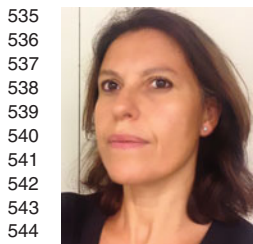
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Optimized Energy Management System to Reduce Fuel Consumption in Remote Military Microgrids

Norma Anglani, Giovanna Oriti, and Michele Colombini

Abstract—This paper presents an optimized energy management system (OEMS) to control the microgrid of a remote temporary military base (FOB) featuring diesel generators, a battery energy storage system (BESS), and photovoltaic (PV) panels. The information of the expected electric demand is suitably used to improve the sizing and management of the BESS, according to the days of operation. The OEMS includes power electronics to charge the batteries from either the PV source or the diesel generators, and it can function as a current source when it is supplementing the power from one of the generators or as a voltage source when it is the sole source of power for the loads. The new contribution of this paper includes the optimization of a FOB's microgrid, where critical loads must be serviced at all times. The proposed optimization, which uses Special Order Sets for the semicontinuous function handling, also integrates economic evaluations by properly taking into account how the size of BESS affects its charge/discharge cycle; thus, the FOBs' battery lifetime, in addition to its fuel consumption. Results from optimization are employed by the OEMS to coordinate the energy sources, and match the critical and noncritical loads with the available supply. Fuel savings of $\approx 30\%$ (and $\approx 50\%$ adding the PV source) can be achieved with respect to the already improved, but not optimal, solution of a previous work.

Index Terms—Energy management system (EMS), microgrid, mixed integer linear optimization (MILP), rain flow counting method, renewables integration, Special Ordered Set (SOS).

I. INTRODUCTION

RECENT emphasis on energy efficiency has stimulated the use of smart hybrid power supply systems in remote military camps such as the U.S. Marine Corps forward operating bases (FOBs) [1], [2], also in view of new electrifying paradigms [3]. Reducing fuel consumption results both in reduced operational cost for the FOB, and it can also save soldiers' lives because fuel transportation is dangerous, especially outside U.S. borders. Recently developed FOBs' power systems include a

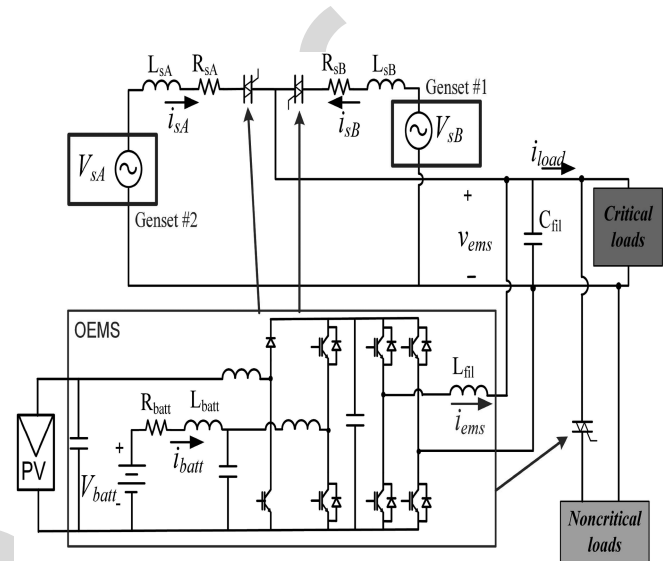


Fig. 1. Optimized energy management system architecture.

battery energy storage system (BESS) and renewable energy sources such as photovoltaic (PV) panels in addition to traditional diesel generators [4]. In [2], a power electronics based energy management system (EMS) was used to significantly reduce fuel consumption in a power system featuring two diesel generators and a BESS; however, the study did not consider the BESS state of charge (SOC), lifetime, cost, or the addition of PV sources recently introduced in FOBs. In this paper, an optimized EMS (OEMS) is presented where a simple but robust algorithm manages the diesel generators, the BESS, and PV source as shown in Fig. 1.

Critical loads in the schematic are those electrical devices that must be powered at all times to ensure the success of the military operation. The optimization strategy includes lifetime and economic considerations for the BESS; thus, managing the cost of the microgrid while reducing fuel consumption. Applications of online and offline optimization techniques in the management of energy supply and demand are widely available as in [5], [6], and [7] and more recently in [8] and [9]. They are applied not only to microgrids, as in [10], but also to assess the impact on bigger energy system, as in [11]. Although some of these papers deal with critical load service and fuel consumption, none of them addresses remote military microgrids and their key issues. In the knowledge of the authors, few examples have been able to achieve such amount of savings, by making the optimization problem as simple as it is shown. Supported by the work of Camponogara *et al.* [12], with respect to the use of the Special

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65 Ordered Sets (SOSs) and by the work of Tankari *et al.* (2013)
 66 in the use of the rainflow counting method [13], we tailored the
 67 algorithms and match them together to find a solution to the
 68 problem of minimizing the fuel consumptions of the FOBs and
 69 optimize the BESS size, according to the operating days. No pre-
 70 vious work solved the specific problems of a FOB, except [14],
 71 which proposes the use of HOMER, but with different purposes.
 72 In this paper, a well-known mixed integer linear programming
 73 (MILP) formulation is proposed for the OEMS. Although MILP
 74 is less sophisticated than other algorithms available in the litera-
 75 ture, analysis shows that its robustness is a fundamental asset to
 76 speed up controlling strategies and obtain satisfactory results.

77 The new contribution of this paper includes the overall opti-
 78 mization procedure which uses SOSs for the semicontinu-
 79 ous function handling, and integrates economic evaluations by
 80 properly taking into account how the size of BESS affects its
 81 charge/discharge cycle; thus, the battery lifetime. Another new
 82 contribution is the hardware implementation of the optimized
 83 control system; in a laboratory prototype the OEMS coordinates
 84 the energy sources and BESS to service critical and noncritical
 85 loads using the results from the proposed optimization. It should
 86 be noted that the application of microgrid technology to FOBs is
 87 rarely found in the literature, therefore this paper is also new in
 88 the application that it presents. One important variable that must
 89 be considered in a FOB is that critical loads must be serviced
 90 at all times, even if this results in shedding of noncritical loads
 91 when a fault occurs. With the proposed algorithm, we operate
 92 to avoid the shedding. Two optimized scenarios, with and with-
 93 out a PV source, demonstrate fuel savings of $\approx 30\% - 50\%$,
 94 respectively, compared to previous work [2]. The scenarios ap-
 95 proach supports a sensitivity analysis on the amount of savings,
 96 when the PV production may fail. Experimental measurements
 97 demonstrate the OEMS functionality.

98 In Section II, the power electronics based OEMS will be
 99 illustrated. In Section III, the formulation of the optimization
 100 problem, the methodology based on SOS-constraints, and the
 101 rainflow counting method are presented to solve the minimiza-
 102 tion of the fuel consumption and for the optimal sizing of the
 103 BESS. The case study and the sizing are described and solved
 104 in Section IV, according to the operating days, conclusions are
 105 drawn in Section V.

106 II. POWER ELECTRONICS BASED EMS

107 The EMS depicted in Fig. 1 includes three inverter legs and
 108 a field programmable gate array (FPGA) based control system.
 109 Two of the legs are used for a bidirectional H-bridge converter
 110 which converts power from the dc bus to the ac loads and vice-
 111 versa. The other two legs are used for the battery pack and
 112 PV panels, respectively. Since the PV source power flows uni-
 113 directionally, only one switch and one diode of the fourth in-
 114 verter leg are used for the boost converter that conditions the
 115 PV power. The EMS includes a primary controller [15] for the
 116 power electronics and a secondary controller to manage the
 117 loads and distributed resources, including storage and PV. Solid
 118 state switches are used to connect and disconnect the two gener-
 119 ator sets (gensets) and the noncritical loads, which can be shed

120 if there is a power failure or to control peak power consumption.
 121 While Oriti *et al.* [15] focus on the EMS primary control sys-
 122 tem, this paper focuses on the secondary controller which gives
 123 the OEMS the ability to optimally manage loads and the BESS
 124 SOC.

125 III. PROBLEM FORMULATION: MILP, SOSs, AND THE 126 RAINFLOW COUNTING METHOD

127 In the following, we explain how we combine two techniques
 128 to provide an optimized secondary control law, able to answer
 129 the questions.

- 130 1) Which is the best configuration to save fuel and size bat-
 131 teries in a FOB, according to the number of operating
 132 days?
- 133 2) Which is the range of savings, if PV panels are used?
- 134 3) How can we realize it?

135 At first, we propose a formulation which improves the origi-
 136 nal setup reported in [2], second, we evolve toward a hybrid
 137 microgrid configuration, by adding the new PV plant and finally
 138 we optimize the size of the battery according to the economics
 139 and the life time of the microgrid (i.e., the operative days of
 140 the base). The results of such constrained optimization problem
 141 become instrumental for the OEMS described in the previous
 142 section. We look at a typical day, divided into j th time steps,
 143 then we base our model on two vectors of semicontinuous,
 144 nonnegative decision variables: $x_{1,j}$ and $x_{2,j}$ the average load
 145 factors of genset #1 ($P_{1r}=5$ kW, rated power) and genset #2
 146 ($P_{2r}=15$ kW), as defined in (1.5) of Table I.

147 One interesting feature in our formulation is represented by
 148 the choice to also use, as decision variable, the SOC value at the
 149 beginning of the day and impose to have the same value at the
 150 end of the day. Such choice allows us to take into account the
 151 temporal continuity, while representing a typical day. This is a
 152 neglected aspect in many papers dealing with optimization on
 153 daily profiles, although it is an important one.

154 Fig. 2 reports the linearized relationships between gensets'
 155 consumption (gal/h, 1gal = 3.79 l) and $x_{i,j}$ (and also power).
 156 Data are elaborated from an extensive research on technical
 157 datasheets from several manufacturers' websites like Caterpillar
 158 [16], Cummins [17], Kohler [18], providing gensets of suitable
 159 size for the proposed case study. Although it may seem simple
 160 to draw such relationship, a considerable effort is represented
 161 by how such data are sought and interpreted from technical
 162 datasheets.

163 We formulate an optimization problem to minimize the fuel
 164 consumption of the facility of Fig. 1, that is

$$165 f(x_{1,j}, x_{2,j}) = \sum_{\substack{1 \leq i \leq 2 \\ 1 \leq j \leq J^*}} C_{i,j} = \begin{cases} m_i \cdot x_{i,j} + q_i & \text{when } x_i^m \leq x_{i,j} \leq x_i^M \\ 0 & \text{when } x_{i,j} = 0 \end{cases} \quad (1)$$

166 over a J^* horizon, discretized in j time steps. m_i and q_i are
 167 the coefficients of the two linear equations in $x_{i,j}$ of the upper
 168 Fig. 2. Additional equations describing the working conditions
 169 of the diesel gensets and BESS, also with respect to photovoltaic
 170 availability, are reported in Table I with a succinct description.

TABLE I
 LIST OF VARIABLES, PARAMETERS, AND EQUATIONS DESCRIBING THE PROBLEM CONDITIONS (AT TIME j)

Variable /parameter	Description of var./param. and/or Eq.	Equations	#
$x_{1,j} - x_{2,j}$	dominion of decision variables (i.e., load factors)	$x_1^m \leq x_{1,j} \leq 1$ or $x_{1,j} = 0$	(1.2)
	no syncro condition	$x_2^m \leq x_{2,j} \leq 1$ or $x_{2,j} = 0$	(1.3)
$x_{3,j}$	battery load factor dominion	$x_{i,j} > 0 \rightarrow x_{k,j} = 0 \quad \forall k \neq i$	(1.4)
$P_{i,j}$	power from gen. and from/to BESS at time j	$-1 \leq x_{3,j} \leq 1$	(1.5)
	$(P_{1r}, P_{2r}, P_{BATmax})$	$x_{i,j} = \frac{P_{i,j}}{P_{ir}}$	(1.6)
T_{bat}, E_{bat}	time of discharge at rated P_{BATmax} and capacity of BESS	$E_{bat} = P_{BATmax} \cdot T_{bat}$	(1.7)
$L_j, P_{PV,j}$	Load and available PV power	$x_{1,j} \cdot P_{1r} + x_{2,j} \cdot P_{2r} - x_{3,j} \cdot P_{BATmax} + (P_{PV,j}) = L_j$	(1.8)
SOC_j in %	state of charge	$SOC_j = SOC_{j-1} + x_{3,j} \cdot \frac{j}{T_{bat}}$	(1.9)
	decision var.	$SOC_0 = SOC_{J^*}$	(1.10)
	dominion	$SOC^m \leq SOC_j \leq SOC^M$	(1.10)

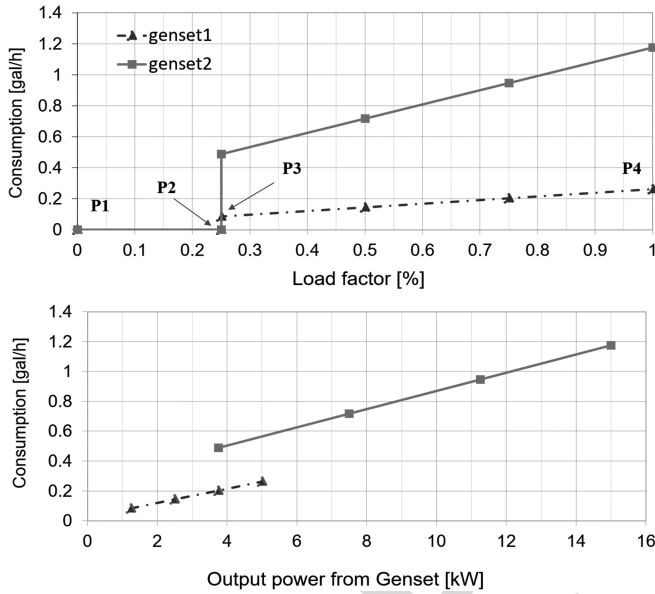


Fig. 2. Fuel consumptions (gal/h) versus load factor (%), or output power in kW for genset #1 $P_{1,r} = 5$ kW and genset #2 $P_{2,r} = 15$ kW. At the top, the coefficients of the linear equations are $m_1 = 0.2366 - q_1 = 0.0253$; $m_2 = 0.9153$. $q_2 = 0.2597$, respectively. Elaboration from [16]–[18].

170 The constraint, involving x_3 a dependant variable, means that
 171 the battery can be charged and discharged (assuming both
 172 positive and negative values), having as its hourly limit $\pm P_{BATmax}$.
 173 This condition is set to preserve its lifetime, besides charging
 174 and discharging efficiencies are set equal to 1.

175 In balancing the supply and the demand side, also the contribu-
 176 tion of the PV source ($P_{PV,j}$) can be taken into account in a
 177 deterministic way, if it exists.

178 If one of the two diesel generators can be used as a backup
 179 power to improve the reliability, no synchronization between
 180 the two gensets is required, at this stage [19].

181 Unfortunately (1) and some constraints in Table I are not
 182 straightforwardly applicable to linear programming solvers like
 183 CPLEX. The objective function (1) is a sum of the consumption

associated with the running of the two gensets

$$\begin{cases} f(x_{1,j}) = 0.2366x_{1,j} + 0.0253 \\ f(x_{2,j}) = 0.9153x_{2,j} + 0.2597 \end{cases} \quad (2)$$

185 in each time frame j th a new $x_{i,j}$ is assessed. $x_{i,j}$ can either
 186 be a value between 0.25 and 1 or be 0, so for each function
 187 $f(x_i)$, four major points can be identified by their coordinates:
 188 $P_i^1(0, 0)$, $P_i^2(0.25^-, 0)$, $P_i^3(0.25^+, m_i \cdot 0.25 + q_i)$, $P_i^4(1, m_i$
 189 $+ q_i)$ (see Fig. 2 where the points are highlighted only for genset
 190 #1). Besides, the no synchronization requirement implies that
 191 at the time j , $\forall i$

$$x_{i,j} > 0 \Leftrightarrow x_{l,j} = 0 \text{ for } l \neq i. \quad (3)$$

To deal with such features on decision variables, the Special
 192 Ordered Sets (SOSs), a tool in the Branch and Bound method to
 193 branch groups of variables, are introduced [20]. SOSs of type 2
 194 are functional to deal with piecewise linear continuous functions
 195 (like the objective function) and type 1 to deal with the no
 196 synchronization requirement as in [21] and [22]. The formulation
 197 of a MILP problem is thus given, from the objective function
 198 of (1) through the definition of all the conditions expressed in
 199 Table I.
 200

A. SOSs Type 2 and Type 1 Resolution

201 $SOS2$ is an ordered set of nonnegative variables, where *no*
 202 *more than two adjacent elements can be nonzero* in a feasible
 203 solution. Consider $f(y)$, the piecewise linear function in y
 204 defined in closed intervals $[\hat{y}_k, \hat{y}_{k+1}]$, where $[\hat{y}_k, f(\hat{y}_k)]$ represent
 205 the coordinates of P_1, \dots, P_K and $k = 1, \dots, K$ (Fig. 3)
 206

y in $[\hat{y}_k, \hat{y}_{k+1}]$ can be written as

$$y = \lambda_k \hat{y}_k + \lambda_{k+1} \hat{y}_{k+1} \quad (4)$$

where

$$\lambda_k + \lambda_{k+1} = 1 \quad \text{and} \quad \lambda_k, \lambda_{k+1} \geq 0. \quad (5)$$

As well, $f(y)$, linear in the interval, can be written as

$$f(y) = \lambda_k f(\hat{y}_k) + \lambda_{k+1} f(\hat{y}_{k+1}) \quad (6)$$

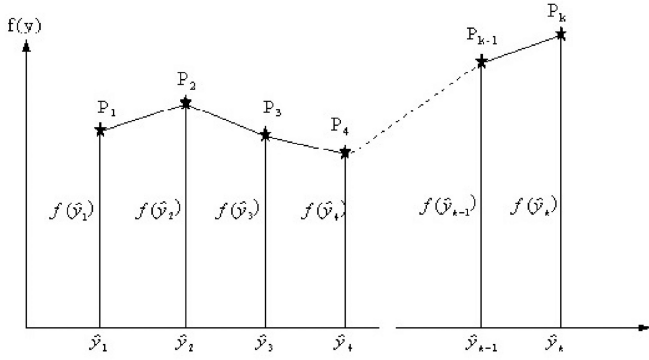


Fig. 3. Generic piecewise linear function $f(y)$ [20].

210 $f(y)$ can be represented by using a set of *weight* variables λ_k ,
 211 $k = 1, \dots, K$ as

$$f(y) = \lambda_1 f(\hat{y}_1) + \lambda_2 f(\hat{y}_2) + \dots + \lambda_K f(\hat{y}_K) \quad (7)$$

212 where

$$\hat{y}_1 \lambda_1 + \hat{y}_2 \lambda_2 + \dots + \hat{y}_K \lambda_K - y = 0 \quad y \geq 0 \quad (8)$$

$$\lambda_1 + \lambda_2 + \dots + \lambda_K = 1 \quad \lambda_k \geq 0 \quad k = 1, \dots, K. \quad (9)$$

213 Besides, we must consider the additional condition that no
 214 more than two adjacent variable can be nonzero at any time
 215 (according to [21] and [22]). These weight variables are the
 216 Special Ordered Set type 2.

217 In an electrical grid, stability is a very important issue as
 218 well as redundancy of the supply system: to provide those two
 219 requirements for a limited supply system like a FOB can be,
 220 where only a few diesel generators exist, we have been assuming
 221 that only one generator is running at a time. Taking into account
 222 such condition requires the use of SOS1. SOS1 are a set of
 223 adjacent subsequent variables where at most one element can be
 224 non zero in a feasible solution. Therefore, (9) under the condition
 225 of SOS1, that only one element can be nonzero, implies that only
 226 one element will be equal to one.

227 B. Rainflow Counting Method

228 The addition of batteries and PV sources to a traditional FOB
 229 power system leads to fuel savings and CO₂ emission reduction.
 230 As the battery size increases the fuel consumption may decrease,
 231 but the overall cost of the microgrid will go up. Therefore,
 232 battery cost and lifetime must be included in the optimization.
 233 In the economic evaluation of a given layout, the real lifetime
 234 of a battery is a sensitive parameter depending on the aging,
 235 according to the charge/discharge cycles and the DoD (Depth
 236 of Discharge). Thus, another step deals with the best sizing of
 237 the BESS, according to the typical daily working cycles. The
 238 chosen approach was an adaptation of the Miner's Rule [23],
 239 introduced by Facinelli in [24]: in brief, he observed that the
 240 higher the DoD the lower the lifetime of a battery (see Fig. 4).

241 Such rule is valid as long as the cycles do not overlap, which
 242 is typical of a simple PV+BESS configuration. When the cycles
 243 are more irregular, then the rule can not be applied as it is.
 244 For instance, this irregularity has been first found in modeling

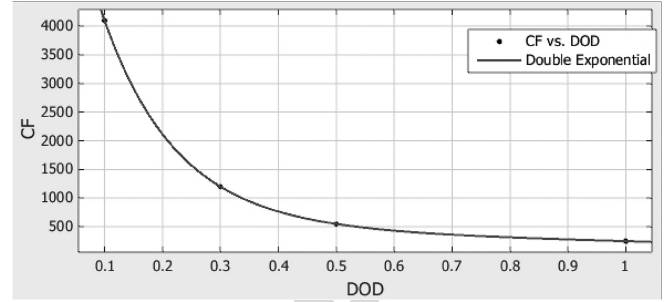


Fig. 4. Fitting curve C_F representing the cycles to failure (lifetime) of batteries versus the fractional DoD, according to data in Table II.

TABLE II
 NUMBER OF CYCLES VERSUS DoD FOR LEAD-ACID BATTERIES [29]

Depth of Discharge	# cycle (approx.)
100%	250
50%	550
30%	1200
10%	4100

Investment Costs: 1kW = 3250\$; 1.5 kW = 4125\$; 3kW = 6750\$; 5 kW=10250\$

wind/diesel kind of systems [25]. If overlapping and irregular
 245 cycles occur, the Rainflow Count, deriving from the original
 246 work of Collins [26], later resumed by [27], [28], and [13], can
 247 be used.
 248

The modeling of the wearing out of batteries due to the cycles
 249 of charge/discharge is based on considering the lifetime (cycles
 250 to failure) depending on the DoD. According to the details in
 251 Table II, the fitting curve is identified and drawn in Fig. 4.
 252

The life fraction is $1/C_F$, if after a given number of cycles
 253 the sum of the number of the cycles (N_i) multiplied by the life
 254 fraction is greater than 1, then the battery is considered being
 255 dead. In other words, the fractional damage D , defined as
 256

$$D = \sum_{i=1}^m \frac{N_i}{C_{F,i}} \quad (10)$$

is the inverse of the lifetime. The unit of measure depends on
 257 how the time horizon cycles are counted: if the DoD cycles are
 258 evaluated on a single day, then the lifetime of the battery is
 259 counted in days. The lead-acid battery characteristics of Sec-
 260 tion IV are from [29] and are reported in Table II, along with
 261 some costs, useful in the case study.
 262

The technique is based on the work of Downing *et al.* [30]
 263 and uses an algorithm created by Nielsony in MatLab code [31],
 264 where individual cycles and the range of cycles of batteries are
 265 assessed according to what is detailed in Section IV. Although
 266 the method is conceptually reasonable and it consists of the
 267 separation of cycles it must be pointed out that there is no
 268 experimental validation of it.
 269

270 IV. RESULTS FOR THE CASE STUDY OF A FOB

This section demonstrates that the optimized algorithm em-
 271 bedded in the OEMS' secondary controller reduces the overall
 272

TABLE III
RELEVANT INPUT AND OUTPUT DATA FOR BOTH THE SCENARIOS (ON A
TYPICAL DAY $J^* = 24$)

Description	Scenario n.1 (no PV)	Scenario n.2 (with PV)
$x_{1,j} - x_{2,j}$	0 or 0.25 ÷ 1 (semicont.)	0 or 0.25 ÷ 1 (semicont.)
$x_{3,j}$	-1 ÷ 1	-1 ÷ 1
$P_{1r} - P_{2r} - P_{BATmax}$ in kW	5 - 15 - 3	5 - 15 - 3
T_{bat} in h (@ $P_{BATmax} = 3kW_P$)	6	6
$SOC^m - SOC^M$ in kWh (and%)	3.6-18 (20%-100%)	3.6-18 (20%-100%)
P_{PV} peak power in kW	0	3
output		
$SOC_0 = SOC_{24}$ in %	40%	100% (see Figs. 9 and 10)
Consump. in gal/day (savings in %)	7.7 (31%)	4.65 (58%) (see Figs. 7 and 8)

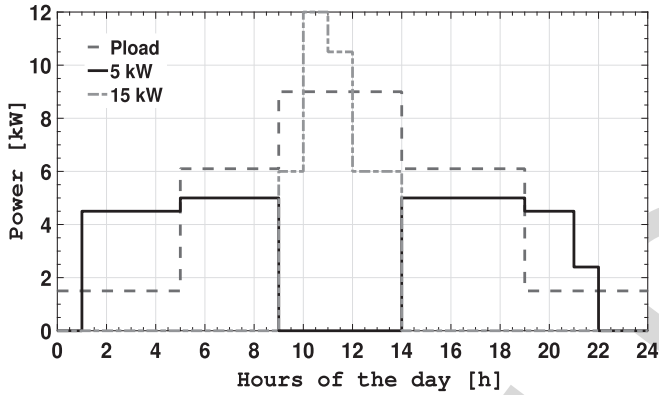


Fig. 5. Scenario n.1: Load and Power from generators (P_{BATmax} equal to 3kW, $SOC_0 = SOC_{24}$, no PV).

273 cost of the microgrid by including battery lifetime expectation
274 and a load management algorithm, more sophisticated than the
275 one presented in [2]. The experimental results are also illustrat-
276 ed.

277 A. Optimization and Cost Analysis: The Two Scenarios

278 In Table III, the most relevant input data are listed for two
279 scenarios: the first without a PV panel, to compare results with
280 the analysis in [2], the second with a 3 kW_P PV panel. At the
281 bottom of Table III, the most important outcomes from the opti-
282 mization are reported: the optimal initial SOC, the consumption
283 (gal/h), and the savings (%) against the original configuration,
284 where 11.2 gal/day (42.4 l/day) were consumed with the same set
285 of electrical loads [2]. We use two scenarios also to perform
286 a sensitivity analysis and to report a range of savings in case the
287 PV panels work or not.

288 The results of the two scenarios are reported in details from
289 Figs. 5 to 10. Figs. 5 and 6 show the power curves over a
290 24 h period for the load, for the two gensets and for the PV
291 source (only in Scenario n.2). In Scenario n.1, both gensets are
292 used but never at the same time; in Scenario n.2, the OEMS
293 chooses to use only genset #1, leaving genset #2 off. This is
294 the result of the optimization algorithm matching the loads to

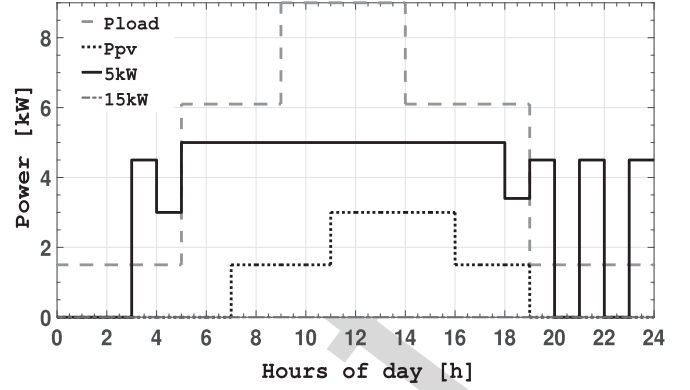


Fig. 6. Scenario n.2: Load and Power from generators (PV and P_{BATmax} both equal to 3kW, $SOC_0 = SOC_{24}$).

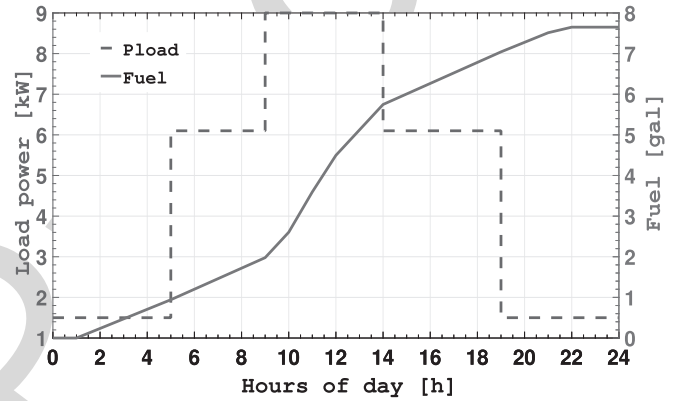


Fig. 7. Scenario n.1: Load and Consumption, power in (kW) on the primary y-axis, consumption in (gal) on the secondary y-axis (P_{BATmax} equal to 3kW, $SOC_0 = SOC_{24}$, no PV).

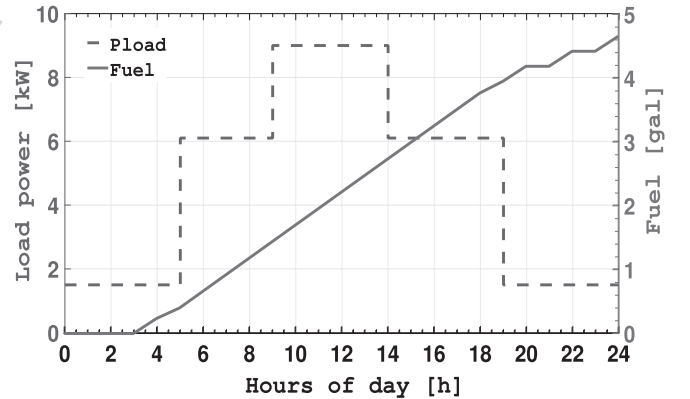


Fig. 8. Scenario n.2: Load and Consumption, power in (kW) on the primary y-axis, consumption in (gal) on the secondary y-axis (PV and P_{BATmax} both equal to 3kW, $SOC_0 = SOC_{24}$).

the sources to minimize fuel consumption, with the addition on
295 security of supply. The fuel consumption over the 24 h period is
296 plotted in Figs. 7 and 8. The total consumed fuel is 7.7 (29.15 l)
297 and 4.65 gallons (17.6 l), which demonstrates in both cases a
298 31% and 58% reduction, compared to the analysis in [2]. These
299 results demonstrate that the 80% derating practice, typically
300 used when sizing diesel generators in FOBs, is not necessary,
301

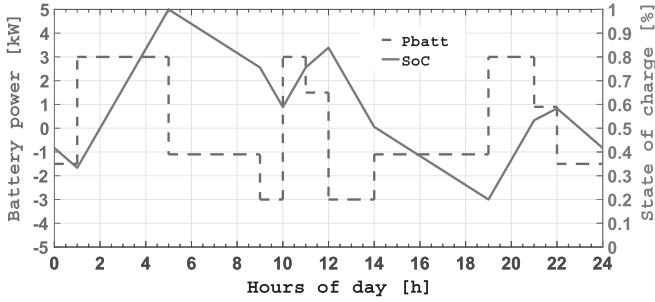


Fig. 9. Scenario n.1: Power from/to Batteries in (kW) (on primary y-axis); SOC [%] (on secondary y-axis) ($P_{BATmax} = 3kW$, $SOC_0 = SOC_{24}$, no PV). On the x-axis the hours of the typical day.

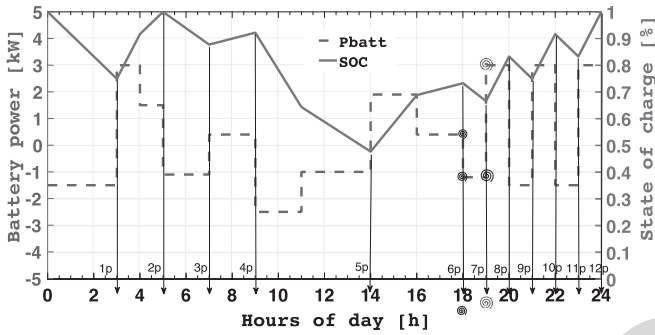


Fig. 10. Scenario n.2: Power from/to Batteries in (kW) (on primary y axis); SOC [%] (on secondary y-axis) (PV and $P_{BATmax} = 3kW$, $SOC_0 = SOC_{24} = 100\%$). On the x-axis the hours of the day and above the peaks count (from 1p to 12p). Signs at time 6 P.M.(18) and 7 P.M. (19) are recalled in Figs. 15 and 16.

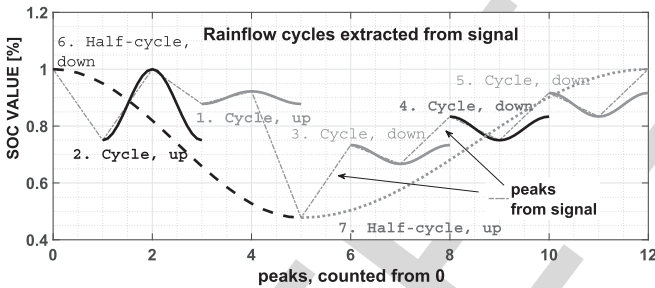


Fig. 11. Scenario n.2: identification and counting of cycles to failure. On the y-axis the SOC in % (the dotted of Fig. 10 and the superimposed peak identification and associated cycle or half-cycle) on the x-axis the peaks count.

302 because a single generator can be used at any given time, leaving
303 the second one as backup.

304 The BESS power and SOC are shown in Figs. 9 and 10, it
305 can be noted that the optimal starting SOC is different (in Sce-
306 nario n.1 is 40%, while in Scenario n.2 is 100%). The Rainflow
307 counting method is applied to the SOC of Scenario n.2 of Fig. 10
308 (on the x-axis one can read both the time of the day and the counting
309 of peaks and valleys, pointed by the downward arrows) and shown
310 in Fig. 11 for the 12 major trends (up and down) deduced
311 from the scenario itself. The changes in the level of the storage
312 is resolved in individual cycles, in a given interval, and used
313 within the model of *cycles to failure* to cumulatively estimate
314 the battery wearing out. Note that the dotted line in Fig. 11
315 is the SOC curve from Fig. 10, on top of which the cycles to

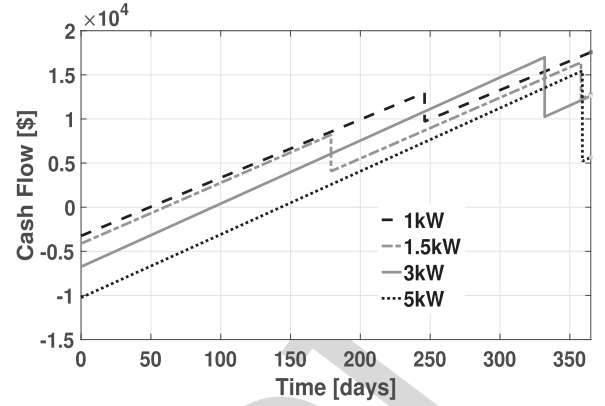


Fig. 12. Scenario n.2 (with $PV = 3kW_p$): Economic evaluation on 365 days: on the y-axis the Cash flow in [\$], on the x-axis the considered horizon [in days] for the four investigated battery sizes, investment costs from Table II and fuel cost 3.964 \$/gal.

failure for the batteries are counted. The results of the Rainflow 316
counting method are combined with the battery data in Fig. 4 to 317
create the cost analysis curves in Fig. 12, where the cash flow 318
of four different BESS sizes (1, 1.5, 3 and 5 kW) are plotted 319
versus the total number of days (the set horizon). We verified 320
and compared how the investment, which depends on the BESS 321
size, is compensated by the saving in fuel over a set horizon, 322
according to 323

$$G(\text{size, horizon}) = -\text{Inv}(\text{size}) + N_F(\text{size}) \cdot C_{\text{fuel}} \cdot \Delta\text{fuel}(\text{size, horizon}) \quad (11)$$

where G the *Gain* is the cash flow in \$, Inv is the investment in \$, 324
 N_F the days to failure of the batteries (depending on the number 325
and DoD of the counted cycles), C_{fuel} is the specific fuel cost 326
(\$/gal) and Δfuel is the daily difference between consumption 327
due to the traditional management of the diesel generators of [2] 328
against the optimized one (in gal/day). In this example, a 365- 329
days horizon is implemented and the 1 kW BESS is identified 330
as the most cost effective configuration because it yields the 331
greatest cash flow at the end of the year. It is worth noting that 332
if the FOB needs to be operative for less than 365 days, for 333
example, in the range between 240 and 300 days, then the 3kW 334
size BESS achieves the highest cash flow and should be used. 335

B. Experimental Set Up and Verification

The objective of this section is to demonstrate how the OEMS 337
hardware executes the commands sent by the optimized sec- 338
ondary controller presented in the previous sections. A scaled 339
laboratory prototype was built and tested that responds to the 340
four different commands. 341

- 1) While the genset is ON, switch from drawing additional 342
power from the battery bank to battery charging mode. 343
- 2) While the genset is ON, switch from battery charging mode 344
to drawing additional power from the battery bank. 345
- 3) Turnoff the genset and transition to battery-only power 346
mode. 347

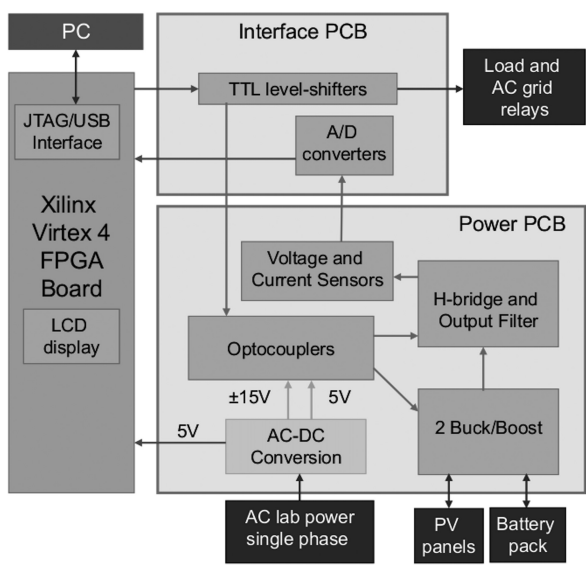


Fig. 13. OEMS hardware block diagram.

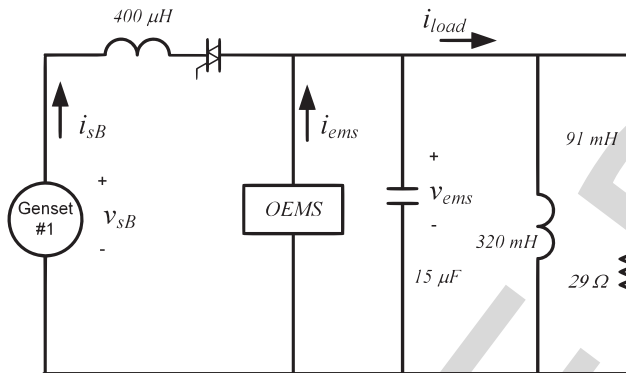


Fig. 14. Laboratory setup.

348 4) Transition from battery-only power mode to the generator
 349 powering the load after the genset is turned ON.

350 The OEMS' secondary controller is responsible for such commands
 351 in either of the two scenarios, with some clarifications
 352 following below. The OEMS laboratory prototype includes an
 353 FPGA development board, a power PCB, and an interface PCB
 354 as shown in Fig. 13.

355 The OEMS power circuit is shown in Fig. 1 and further details
 356 of the hardware implementation and control system can be found
 357 in [15]. The circuit shown in Fig. 14 was assembled in the
 358 laboratory to demonstrate how the OEMS hardware responds
 359 to the secondary controller's commands. The diesel generator
 360 Genset #1 was simulated by the ac grid, which provides a 120 V
 361 rms voltage source, just like a diesel generator would. The power
 362 level of the experiment is a few hundred watts as the main goal is
 363 to demonstrate the hardware functionality, not its power rating.
 364 The dc bus (shown in Fig. 1) was regulated at 200 V and lead
 365 acid batteries were used for the energy storage element.

366 The voltage and current waveforms demonstrating the execution
 367 of the first command of the above list are displayed in
 368 Fig. 15. The load is initially powered by the generator and the
 369 battery together. At $t = 0$, the OEMS reverses the power flow

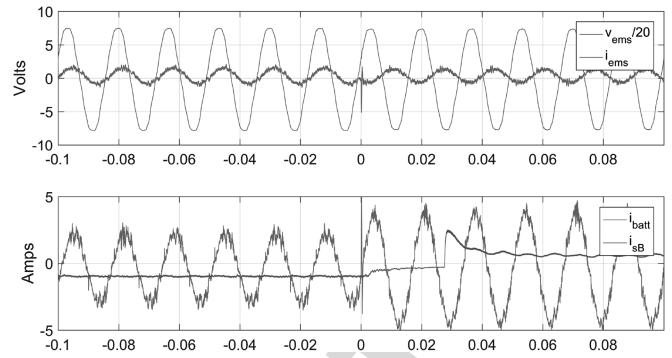


Fig. 15. Transition from drawing additional power from the battery bank to battery charging mode. The generator is kept on (see Scenario n.2 at time 7 P.M. (19:00), small spirals).

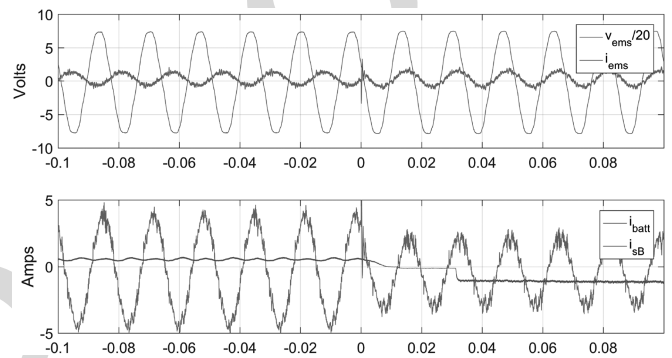


Fig. 16. Transition from battery charging mode to drawing additional power from the battery bank. The generator is kept on (see Scenario n.2 at time 6 P.M. (18:00), small spirals).

370 from/to the battery. The power flow reversal from the battery can
 371 be easily identified in the top plot of Fig. 15, where the OEMS
 372 current i_{ems} has a phase shift of 180° at $t = 0$ when the battery
 373 quits providing power to the load and begins charging the battery.
 374 The bottom plot in Fig. 15, the dc battery current goes from
 375 negative (current out of the battery) to positive (current into the
 376 battery) and the generator current increases to support the load
 377 and the charging of the battery.

378 In Fig. 16, the voltage and current waveforms, demonstrating
 379 the execution of the second command of the list, are displayed.
 380 The power flow reversal is executed by the OEMS in reverse
 381 order with respect to the previous experiment shown in Fig. 15.
 382 Initially, the generator powers the load and charges the battery,
 383 then at $t = 0$ the power flow is reversed and the battery supple-
 384 ments the generator power instead of being charged.

385 The implementation of the third command of the list is dis-
 386 played in Fig. 17, where the generator is turned OFF and the
 387 power to the load comes only from the battery. Once again the
 388 transition is transparent to the load which cannot be disrupted
 389 at any time. Note that an example of this transition occurs in
 390 Scenario n.1 at 9 AM where the additional turn ON of the 15 kW
 391 generator does not turn ON at the same instant as the 5 kW generator
 392 turns OFF, but a few seconds later.

393 In Fig. 18, the voltage and current waveforms demonstrating
 394 the execution of the fourth command of the list are displayed.
 395

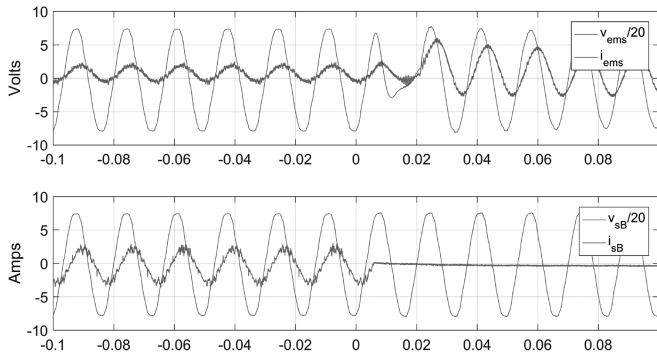


Fig. 17. Disconnect from the generator to transition into battery-only power mode.

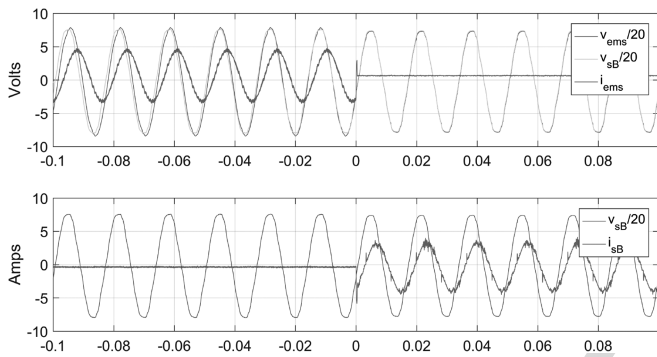


Fig. 18. Step change from battery-only power to battery and generator power after the generator is powered ON.

396 The load is initially powered only by the battery while the OEMS
 397 reduces the phase difference between the generator's voltage and
 398 its own. At $t = 0$, the OEMS latches to the generator's voltage
 399 and the load becomes powered by the generator while the OEMS
 400 current i_{ems} goes to zero. This transition is transparent to the
 401 load. Note that although there is not an example of this transition
 402 in the analyzed scenarios, this is just the first step necessary to
 403 accomplish other transitions, where the battery is subsequently
 404 charged from the generator. The complete transition does not
 405 occur instantaneously as it appears in Fig. 5 and 6, but in steps
 406 that occur within seconds or less.

407 V. CONCLUSIONS AND FUTURE WORK

408 This paper presents an OEMS which minimizes the fuel con-
 409 sumption of the diesel generators used in an FOB's micro-
 410 grid, by addressing several questions, among which the best
 411 BESS size according to the operating days of the FOB. Further-
 412 more, our formulation and solution have demonstrated that the
 413 80% derating practice, typically used when sizing diesel gener-
 414 ators in FOBs, is not necessary, because a single generator can
 415 be used at any given time, leaving the second one as backup.
 416 A MILP formulation, suitably solved by means of SOS2 and
 417 SOS1, has been successfully demonstrated. Its simplicity leads
 418 to robustness and ease of implementation. The Rainflow count-
 419 ing method was used to determine the most cost effective BESS
 420 size with a given operating time, including a 3 kW_P source.

This condition (on given operating times) thus needs to be taken
 into better account for the future operative planning of the basis.

Two 24-h scenarios were analyzed and showed fuel savings
 in the range of 30–50% with respect to a previous improved
 configuration. Such approach provides an estimate of the range
 of fuel savings, should the PV source fail. The analysis of the
 two scenarios shows that, as long as the operating days of the
 FOB are below 240 days or above 300, the best size for the
 BESS is 1 kW (6 kWh capacity), but if the operating days are
 between 240 and 300, the 3 kW battery (18 kWh capacity) is
 the best choice.

A laboratory prototype has been built to demonstrate the
 OEMS functionality. It has also been demonstrated that the
 OEMS can carry out the commands produced by the optimiza-
 tion algorithm without disturbing the bus voltage to which crit-
 ical loads are connected. Future work will analyze the impact
 of adding supercapacitors to the BESS to further increase the
 battery's lifetime and to service unexpected load transients of
 short duration.

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